

The 4th Yamada Symposium on Advanced Photons and Science Evolution, 2010 (APSE 2010)

JICA Osaka, 14-18 June 2010 (Presented on 14 June 2010)

Quantum Nature of Photons and Optical Information

School of Engineering Science, Osaka University

Nobuyuki Imoto

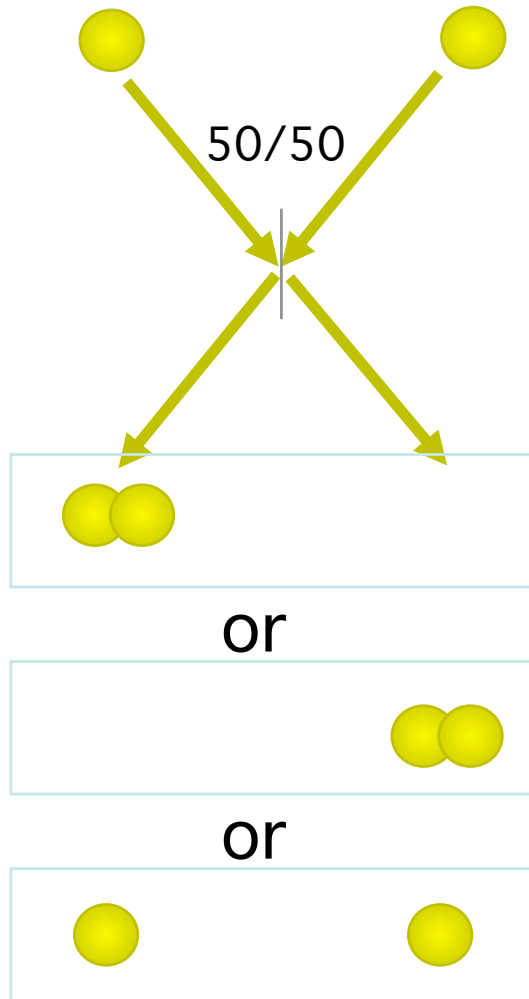


Funding Program for World-Leading
Innovative R&D on Science and
Technology (FIRST Program)

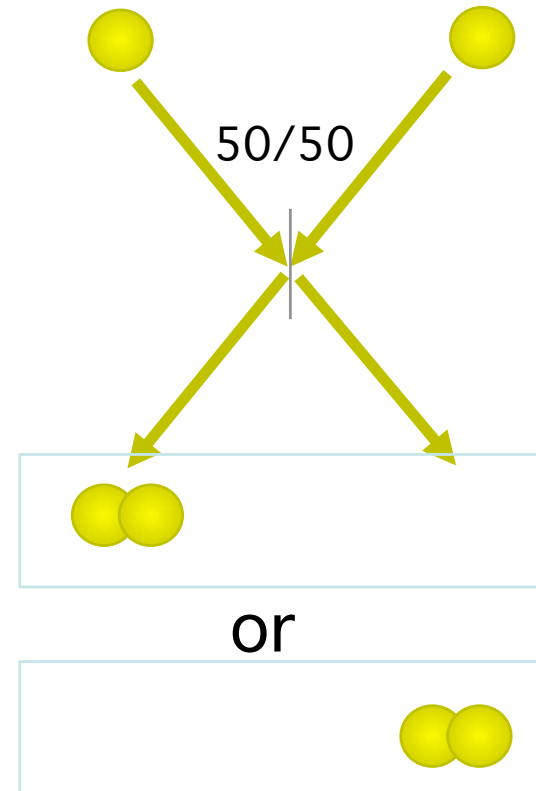
Photons

- Mass-less: moves with velocity c
 - OK for transmission but NG for memories
- Strong or very weak interaction with matters
 - ↓ Low-loss transmission possible
 - Nearly ideal “first-kind measurement” possible
- No direct interaction between photons
 - Linear interaction is strong with the help of matters
 - Nonlinear interaction is weak → a few of those available
- Bosons
 - ▪ Large amplitude possible → wave like
 - ▪ Multi-particle interference
- Feedback oscillation possible (lasers)
 - Easy to prepare in a well-controlled mode
- Spin 1 particles → Polarization (well controlled)

Two-photon interference



truth is...



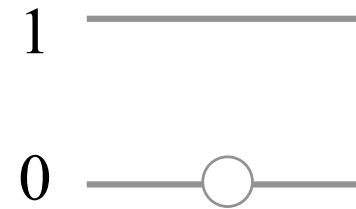
Hong-Ou-Mandel

Bits and Qubits

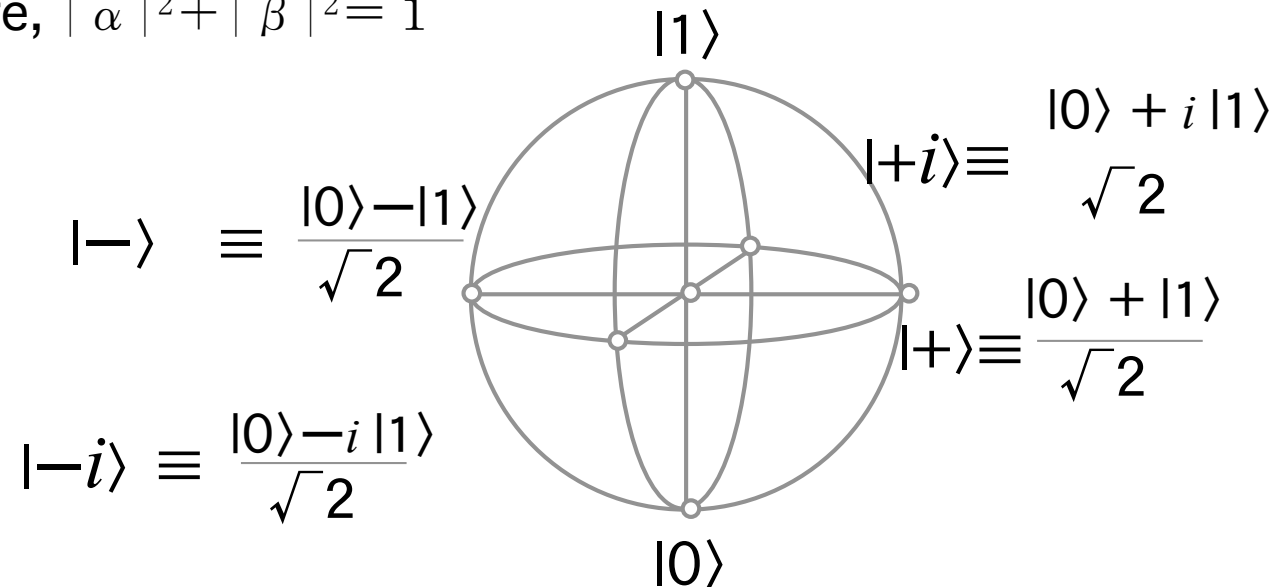
Bit : a system that takes state 0 or 1

A bistability device can be used.

Example: switch, memory



Qubit : a system that takes not only 0 and 1, but also $\alpha|0\rangle + \beta|1\rangle$
 where, $|\alpha|^2 + |\beta|^2 = 1$



Physical systems: photons, atoms, spins, quantum dots, molecules, etc.

Physical object

Qubit variable

Control of qubits

Photon

Polarization

Path

Photon number

Phase

Linear optics

Nonlinear optics

Matter Single atom

ion
spin

SCs

charge
flux

Elementary
excitations

π pulse

$\pi/2$ pulse

Qubit interaction

optical pulse

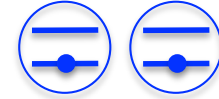
Ensemble of
atoms
etc.

Single photon

External field, etc.

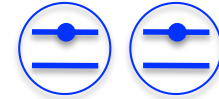
Entanglement among n -partite, m -level systems

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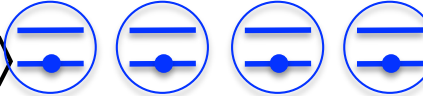
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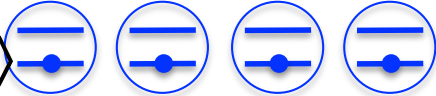
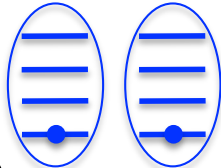
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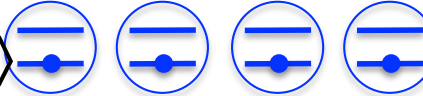
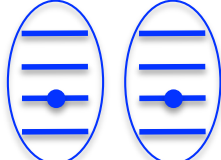
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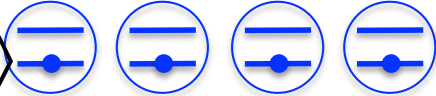
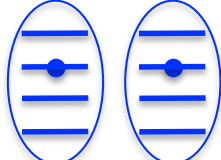
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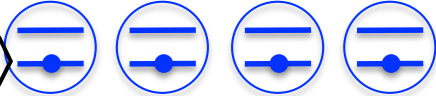
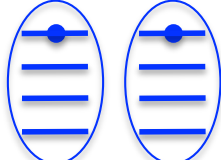
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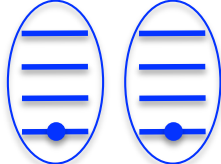
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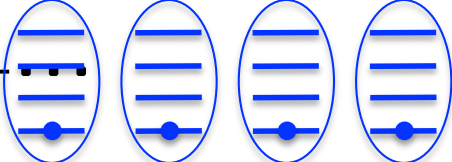
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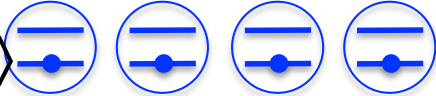
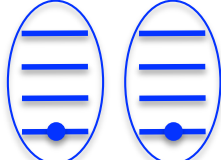
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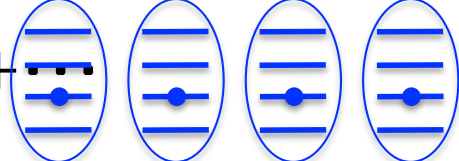
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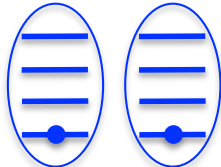
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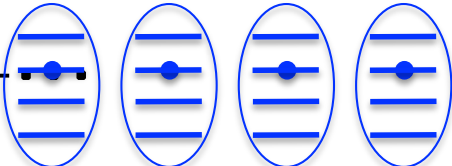
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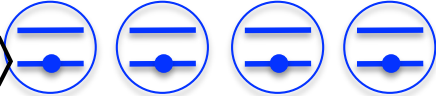
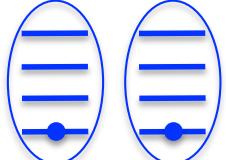
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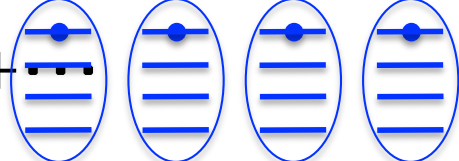
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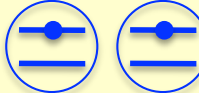
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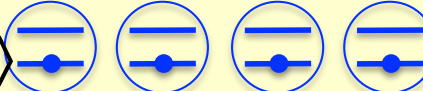
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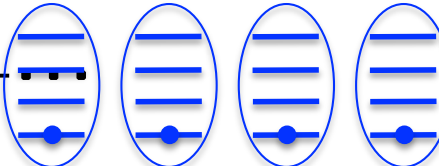
Entanglement among n -partite, 2-level systems

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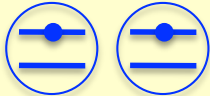
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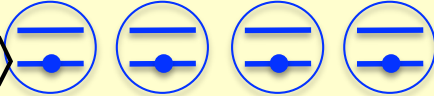
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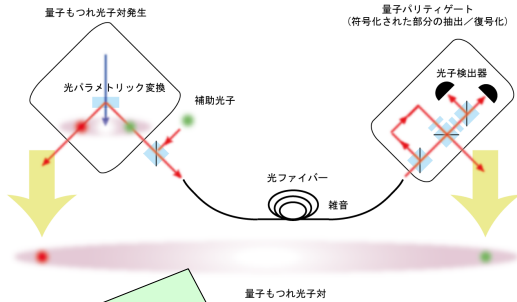
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- difficult to produce (when n is large) \rightarrow a possible direction
- difficult to protect from environmental decoherence \rightarrow a possible direction
- how to use? ex1) cluster-state one-way quantum computation
 ex2) When the meters are entangled \rightarrow Joint weak measurement
 \rightarrow “anomalous weak value”

Our recent activities

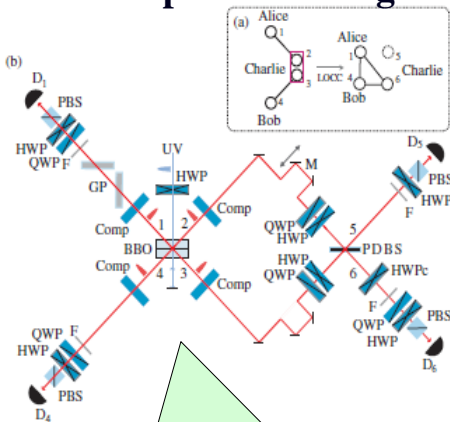
Theory and experiments

Protection of entanglement using DFS (decoherence-free subspace)



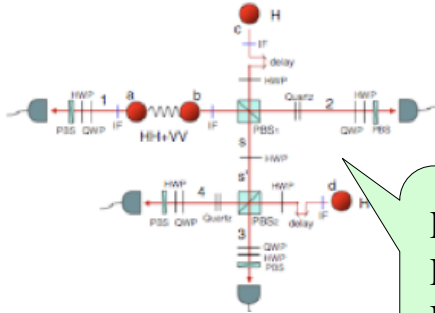
Nature (2003), PRL (2005)
NJP (2007), Nature Photonics (2008)

Fusion gates and expansion gates For multipartite entanglement



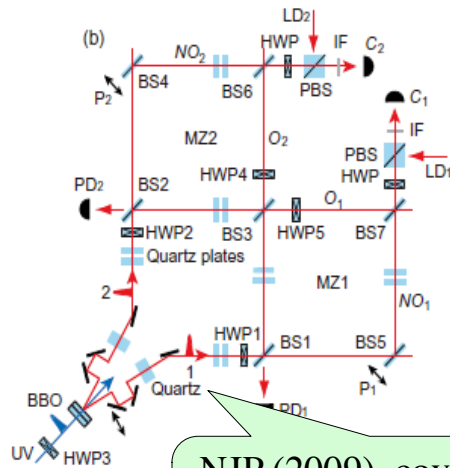
PRL (2009), PRA (2009)
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Cluster-state one-way Quantum computing



PRL (2008)
PRA (2006)
PRA (2005)

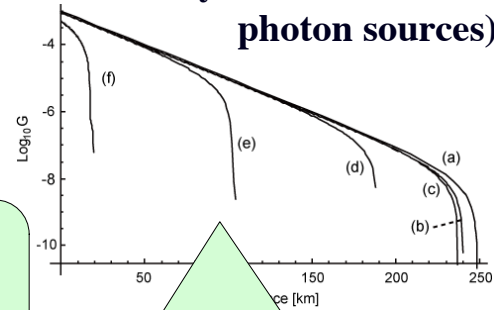
Experimental verification for Aharonov's anomalous weak value



NJP (2009), covered by
The Economist
Wall Street Journal

Theory

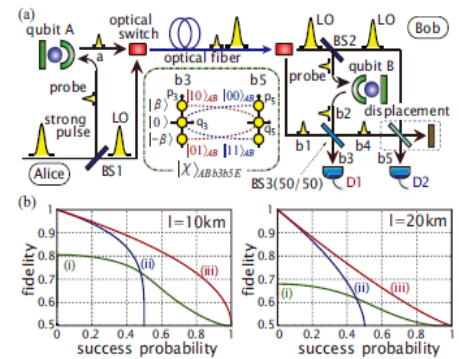
QKD security proof: general theory and for non-ideal photon sources



PRL(2007), PRA(2009)

PRA (2010)
PRA (2009)

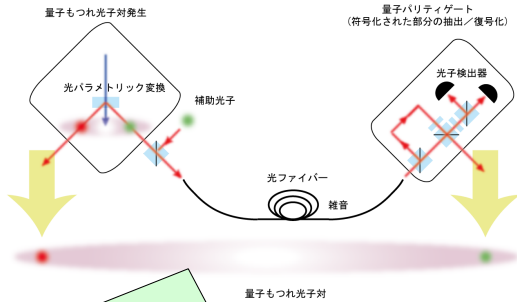
Optimal design for quantum repeaters



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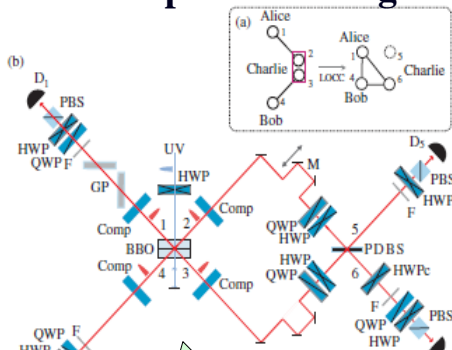
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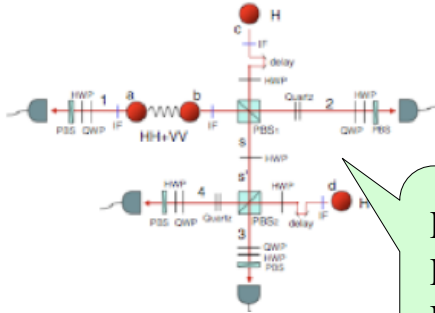
Nature (2003), PRL (2005)
NJP (2007), Nature Photonics (2008)

Fusion gates and expansion gates For multipartite entanglement



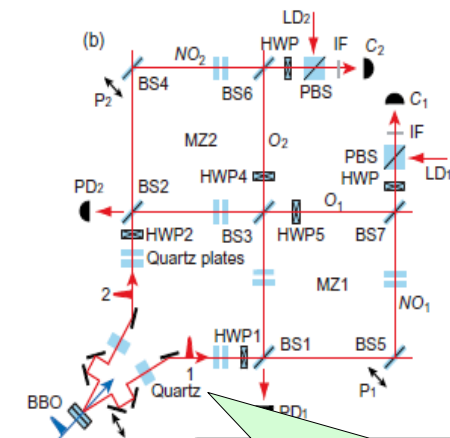
PRL (2009), PRA (2009)
NJP (2009), PRA (2008)

Cluster-state one-way Quantum computing



PRL (2008)
PRA (2006)
PRA (2005)

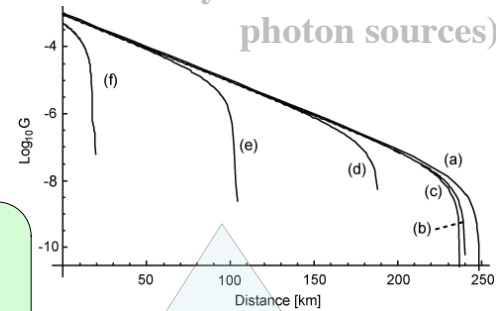
Experimental verification for Aharonov's anomalous weak value



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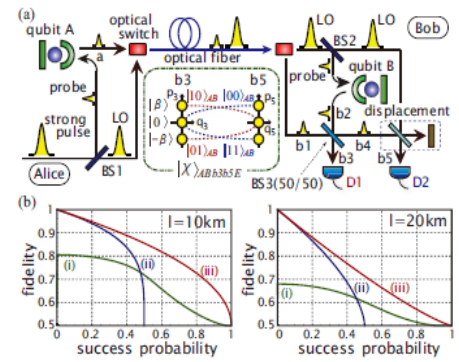
QKD security proof: general theory and for non-ideal photon sources



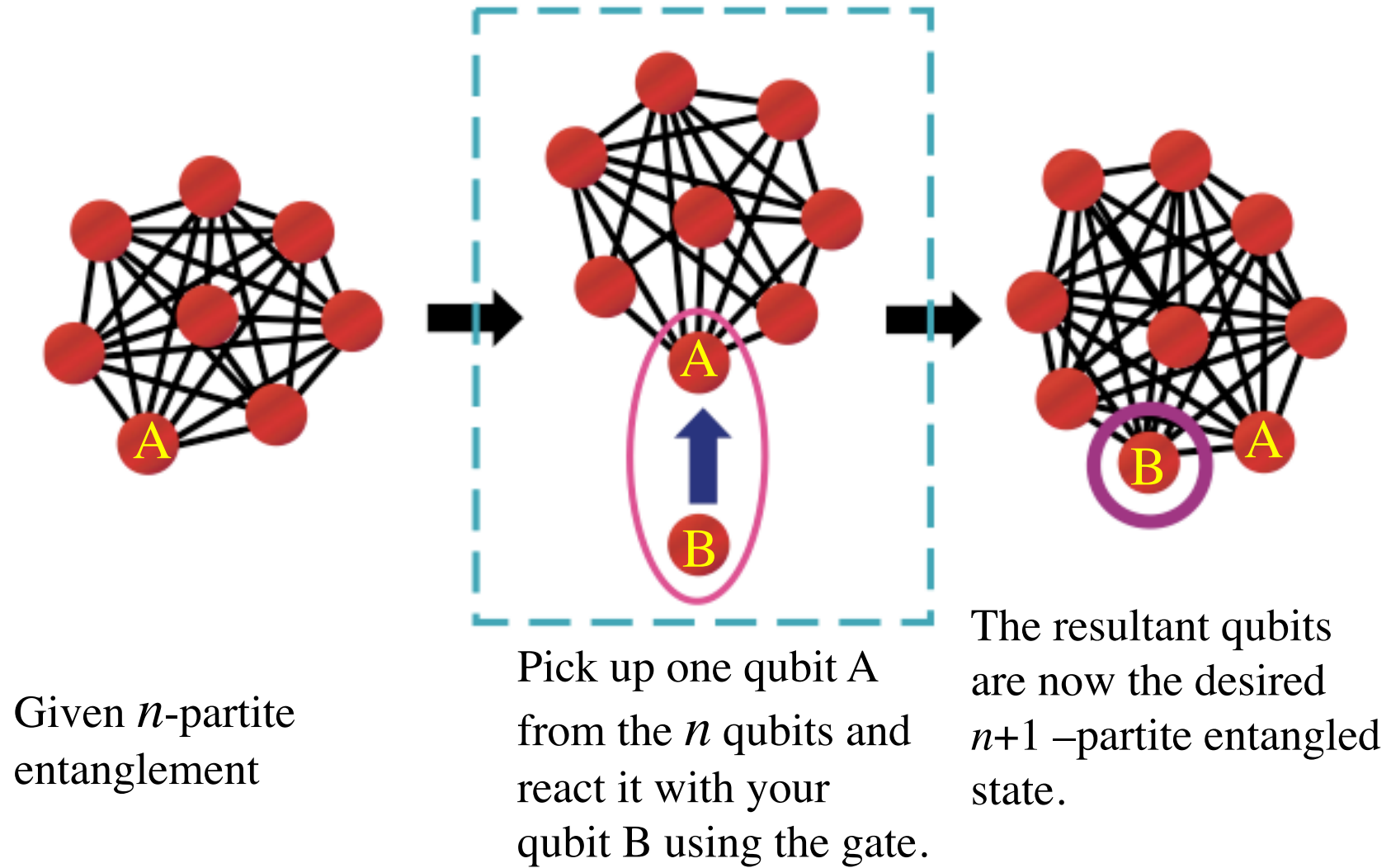
PRL(2007), PRA(2009)

PRA (2010)
PRA (2009)

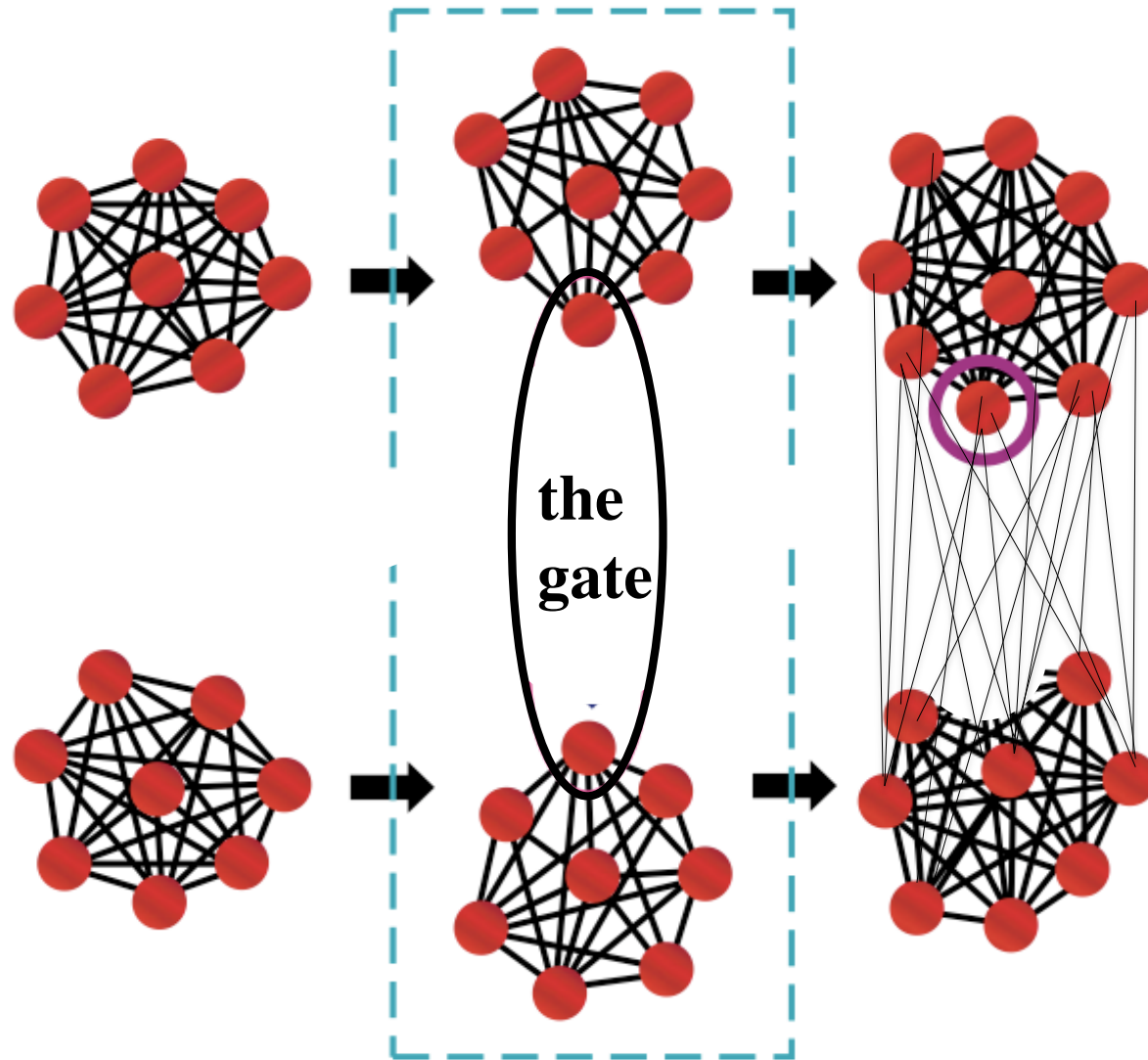
Optimal design for quantum repeaters



An expansion gate



A fusion gate



Question: can do you it deterministically by only accessing one qubit?

Answer: “Yes” for GHZ and cluster states, but “No” for W states.

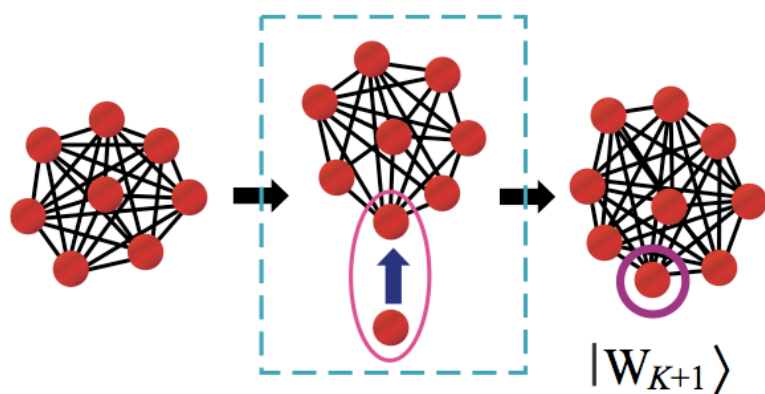
Related work: “persistence of entanglement in W-states” Koashi+Buzek+N.I. (2001 PRA)

Question: is it possible to do it *probabilistically* for W states?

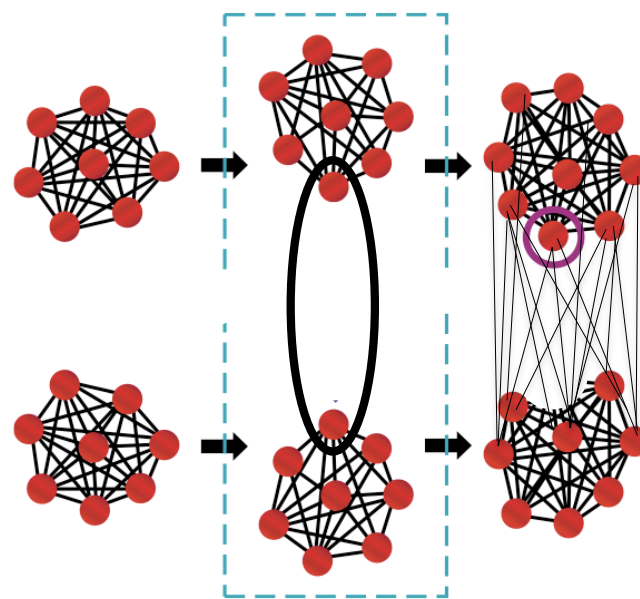
Answer: Yes! Even using linear optics + photon counting.

(\rightarrow papers [1][2][3] in the next viewgraph)

An expansion gate



A fusion gate



T. Tashima, S. K. Ozdemir, M. Koashi, T. Yamamoto, N.I. etc.

[1] Theoretical proposal of a simple expansion gate for “ $n \rightarrow n+2$ ” W states
PRA77, 030302(R) (2008).

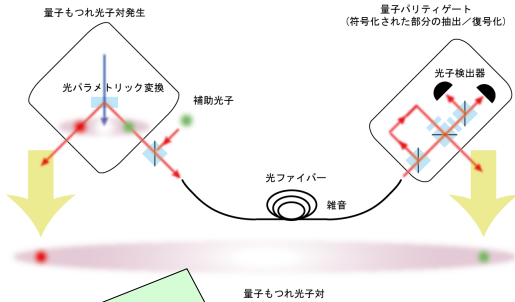
[2] Theoretical proposal of a simple expansion gate for “ $n \rightarrow n+1$ ” W states
New J. Phys. 11, 023024 (2009).

[3] Proposal of a simple fusion gate for W states and experimental verification of the gate by $W_2+W_2 \rightarrow W_3 + 1$ photon detection
Phys. Rev. Lett. 102, 130502 (2009).

Our recent activities

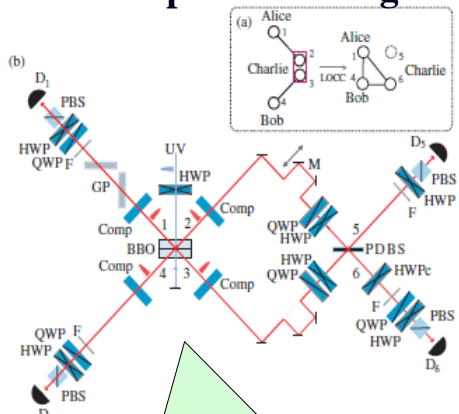
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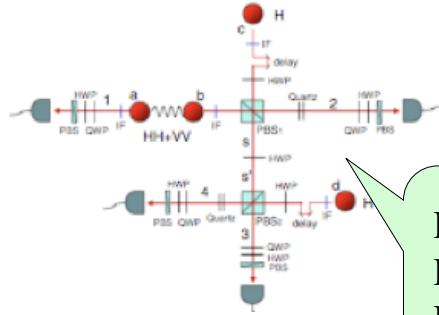
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Fusion gates and expansion gates For multipartite entanglement



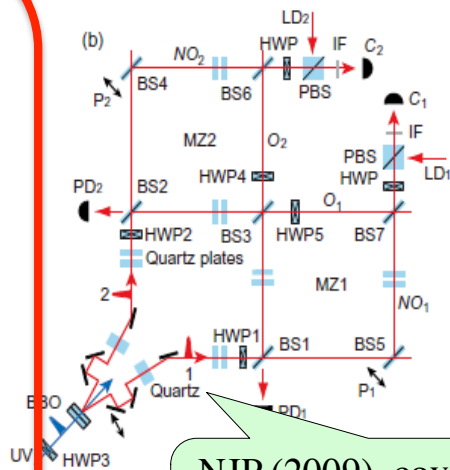
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PRA (2006)
PRA (2005)

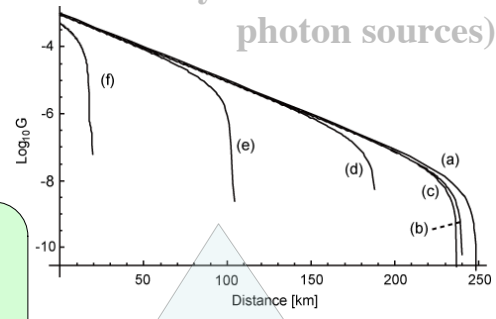
Experimental verification for Aharonov's anomalous weak value



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Theory

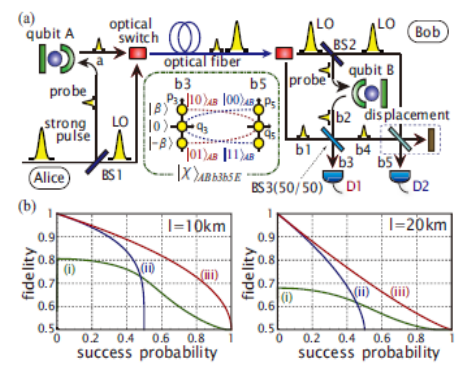
QKD security proof: general theory and for non-ideal photon sources



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PRA (2010)
PRA (2009)

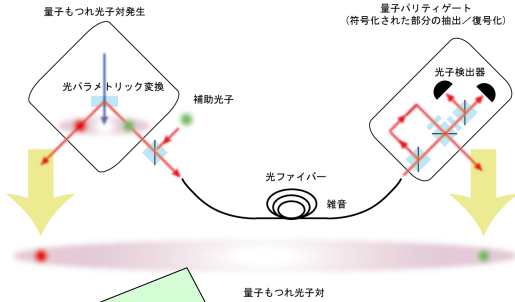
Optimal design for quantum repeaters



Our recent activities

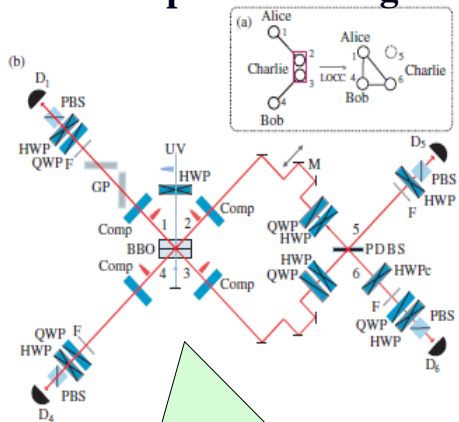
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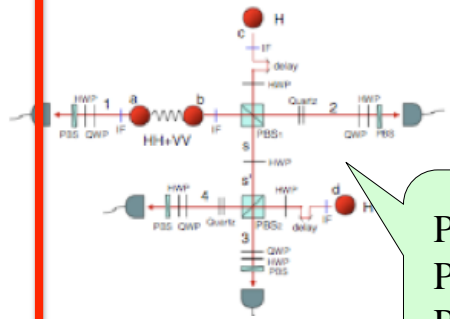
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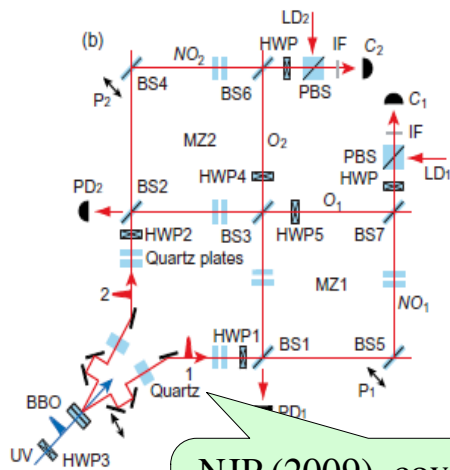
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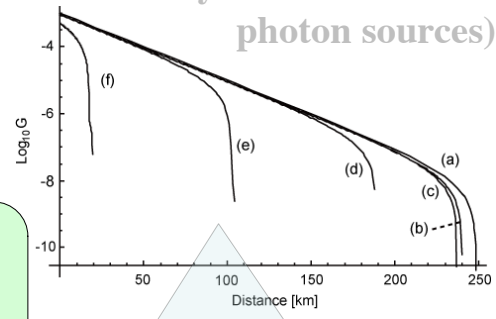
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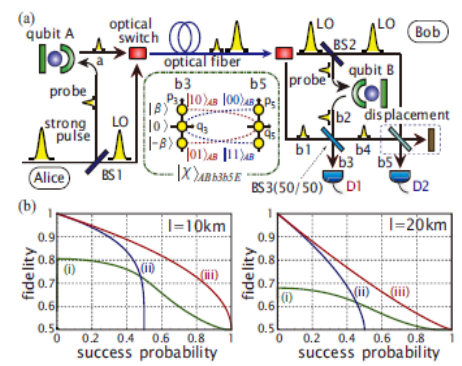
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PRA (2010)
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Errors in a qubit

Polarization of a photon:

H,	V,	45degree
↑	↑	↑
0	1	superposition

Errors: bit/phase/both · · · Pauli matrices

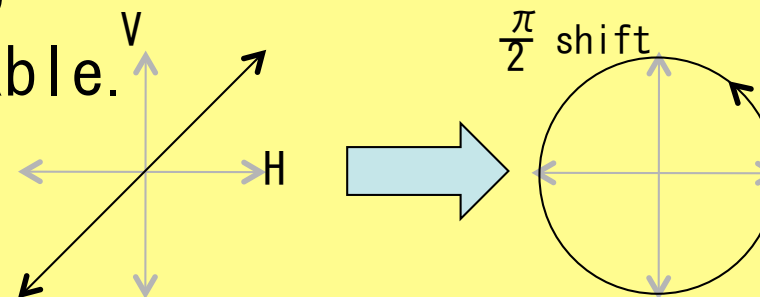
General error correction: Q error correcting codes

(1) needs 5 (or more) physical qubits for 1 logical qubit.

(2) assumes at most 1 error until next correction time.

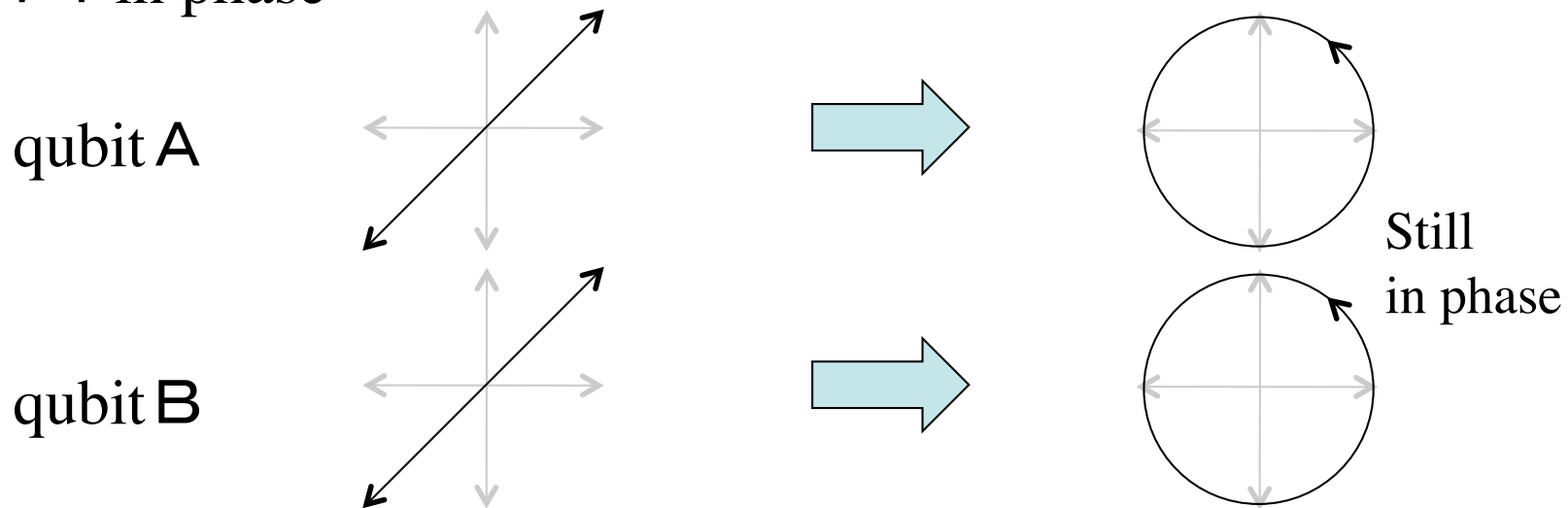
In an optical fiber, phase error is important.

Phase change between two polarization uncontrollable.

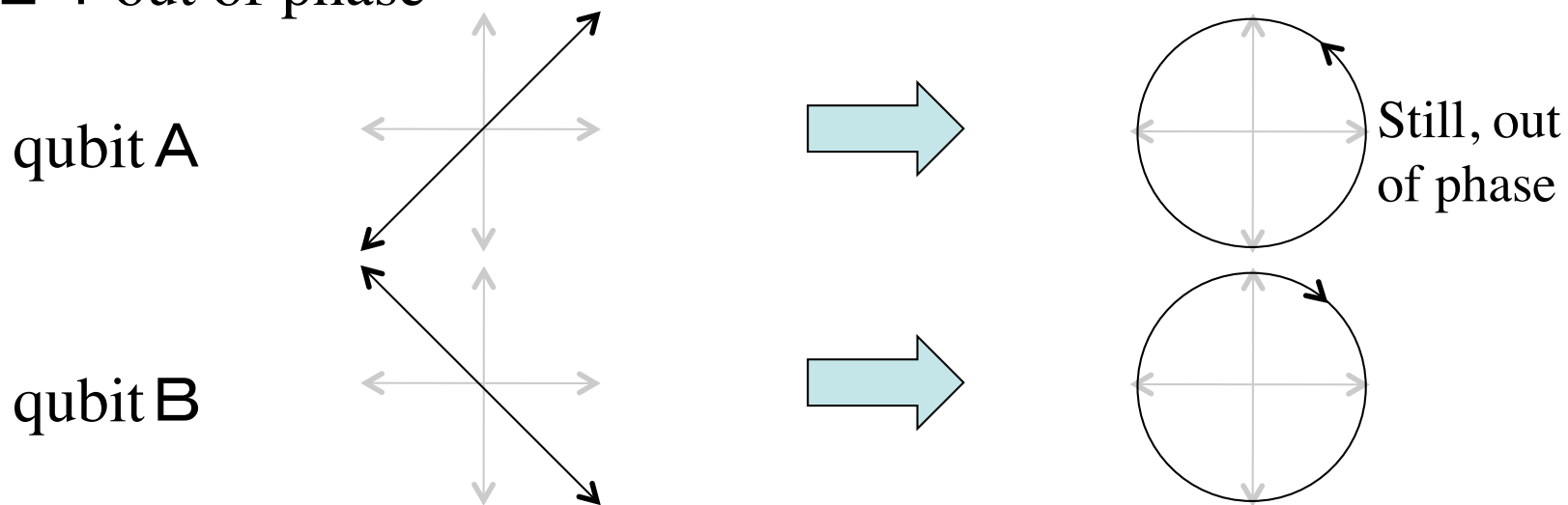


Use of two qubits for 1 logical qubit

case 1 : in phase

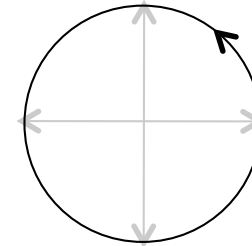
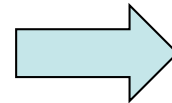
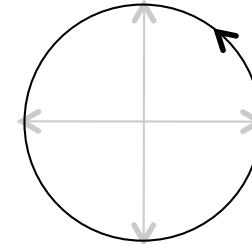
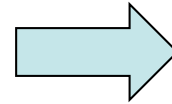
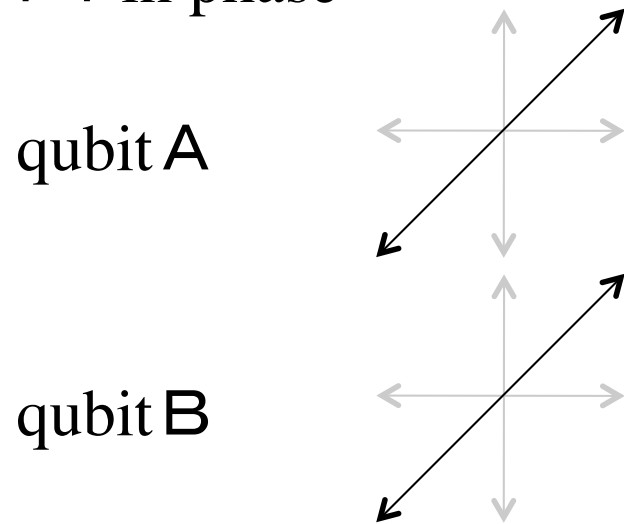


case 2 : out of phase



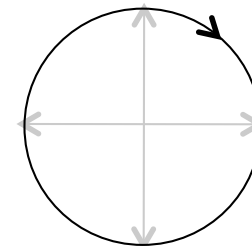
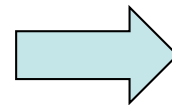
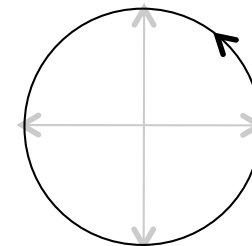
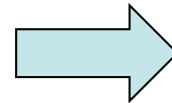
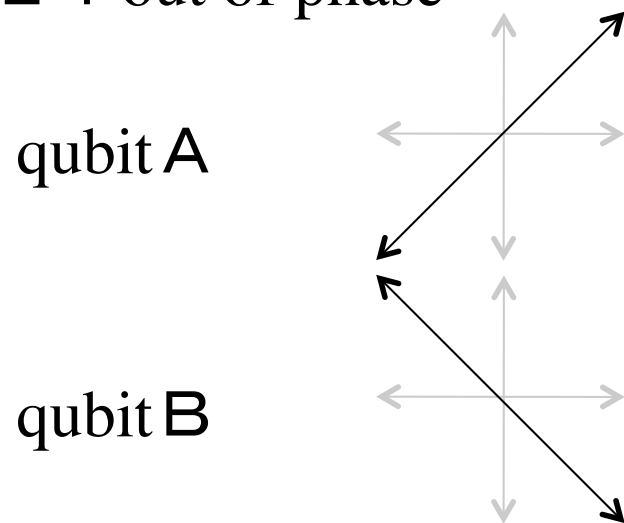
Redefine “in phase” as “0” and “out of phase” as “1”

case 1 : in phase



No error

case 2 : out of phase



It is easy if we can prepare the two physical qubits from the beginning.

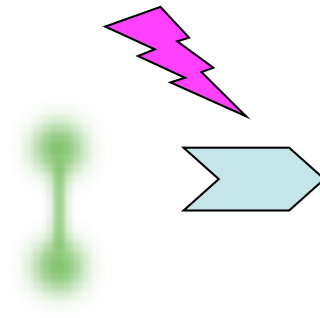
The input logical qubit is given as a physical qubit.

We need to encode it into the DFS of two qubits without observing.

Input qubit that might
be entangled with
the third party



coding



DFS



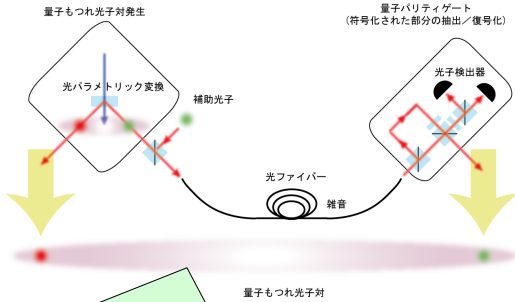
decoding



Our recent activities

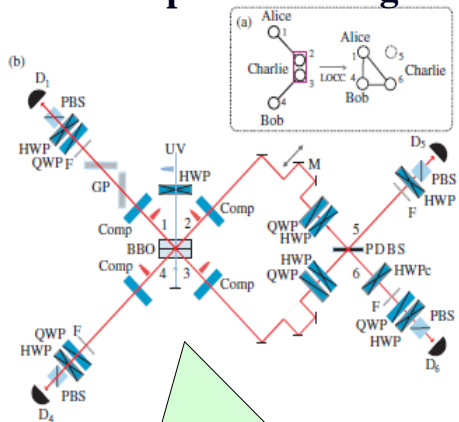
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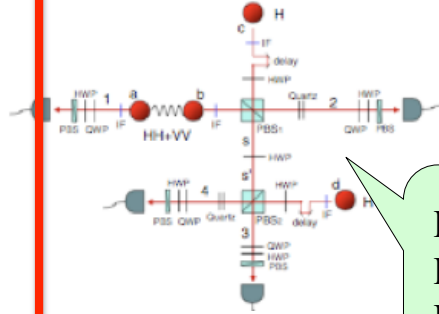
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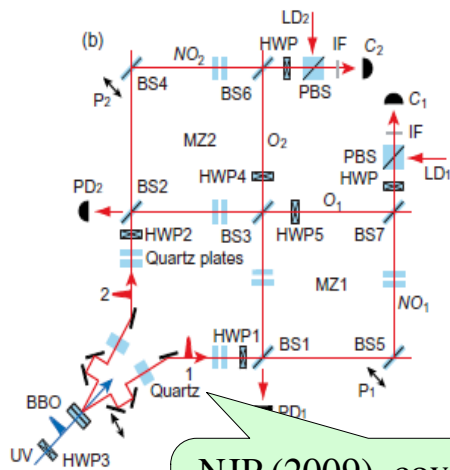
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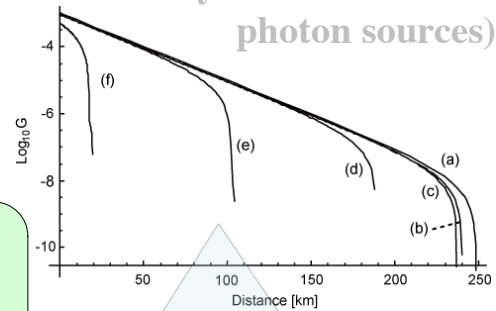
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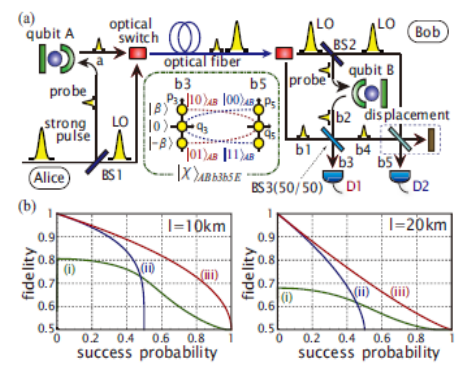
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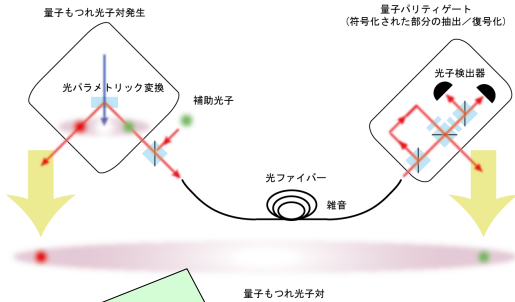
Optimal design for quantum repeaters



Our recent activities

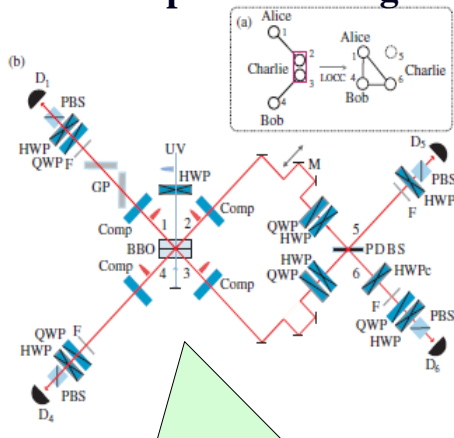
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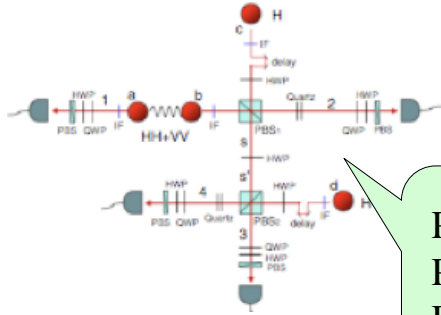
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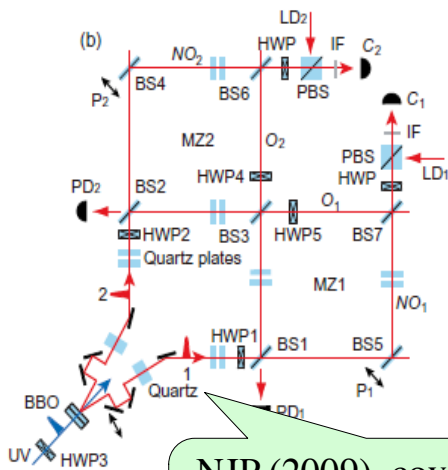
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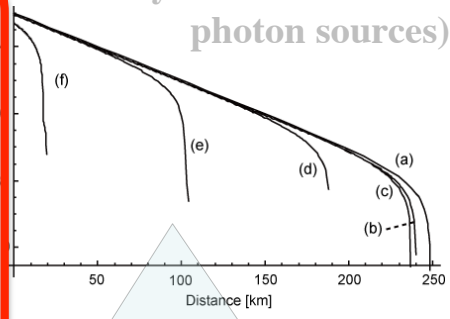
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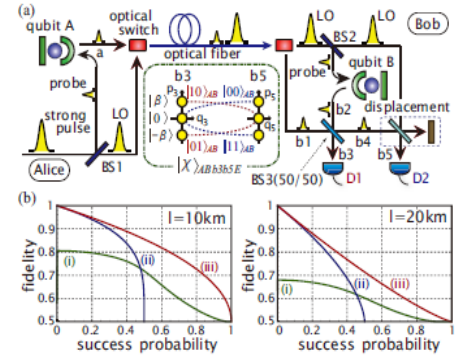
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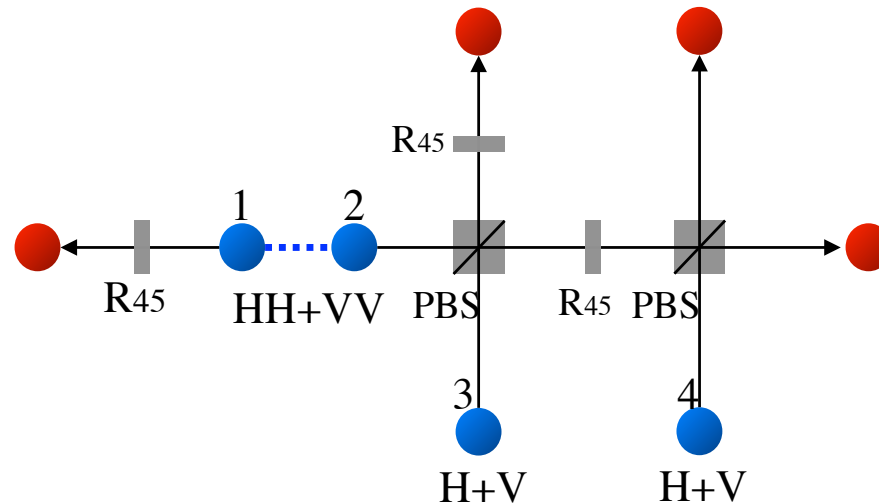
Optimal design for quantum repeaters



4-photon cluster state generation

Simple generation scheme for $|C_4\rangle$

Tokunaga *et al* PRA71, 030301R(2005)



- No need of interferometer stabilization
- High success probability: $1/4$ ($1/9$ before)

Tokunaga *et al* PRL100, 210501 (2008).

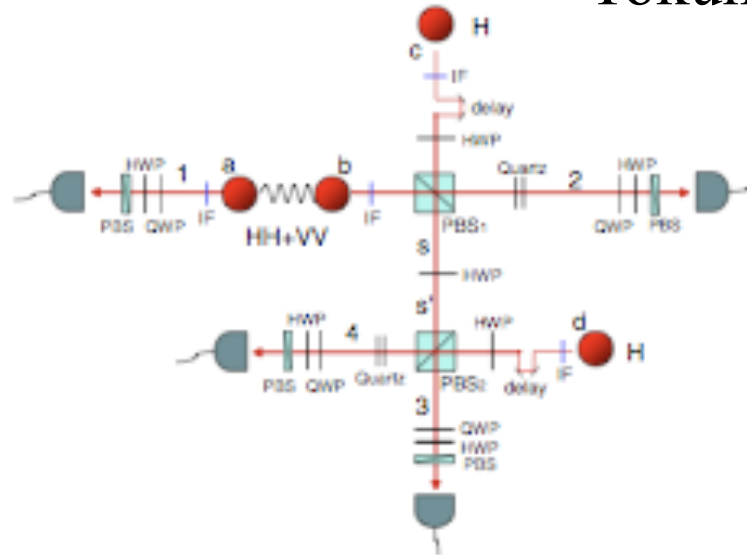


FIG. 1 (color online). Experimental setup for preparing $|C_4\rangle$.

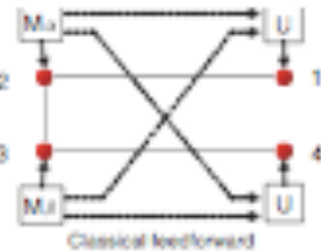


FIG. 4 (color online). Physical implementation and the quantum circuit of a two-qubit gate.



TABLE I. Output state fidelities of two-qubit gates.

α	β	Output state	Fidelity
0	0	$ \phi_1\rangle = H\rangle +\rangle + V\rangle -\rangle$	0.831 ± 0.033
0	$\pi/2$	$ \phi_2\rangle = H\rangle R\rangle + V\rangle L\rangle$	0.847 ± 0.036
0	π	$ \phi_3\rangle = H\rangle -\rangle + V\rangle +\rangle$	0.924 ± 0.025
0	$-\pi/2$	$ \phi_4\rangle = H\rangle L\rangle + V\rangle R\rangle$	0.899 ± 0.028
π	0	$ \phi_5\rangle = H\rangle +\rangle - V\rangle -\rangle$	0.912 ± 0.028
π	$\pi/2$	$ \phi_6\rangle = H\rangle R\rangle - V\rangle L\rangle$	0.913 ± 0.028
π	π	$ \phi_7\rangle = H\rangle -\rangle - V\rangle +\rangle$	0.925 ± 0.024
π	$-\pi/2$	$ \phi_8\rangle = H\rangle L\rangle - V\rangle R\rangle$	0.910 ± 0.027

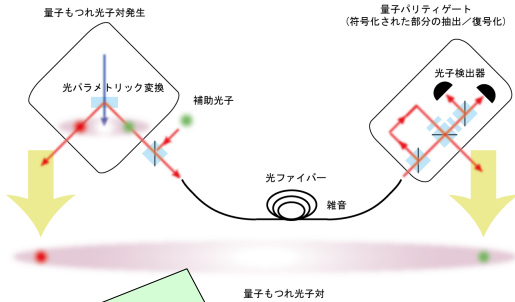
Fidelity (experiment)
 $= 0.895 \pm 0.010$
 > 0.854 (classical limit)

First to exceed the
classical limit

Our recent activities

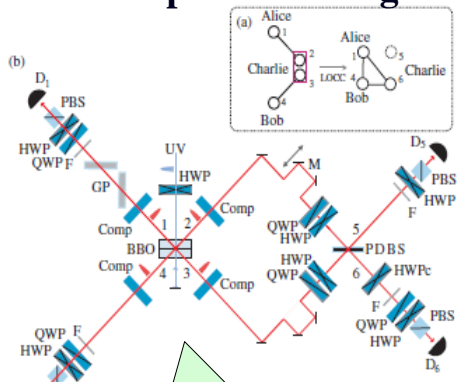
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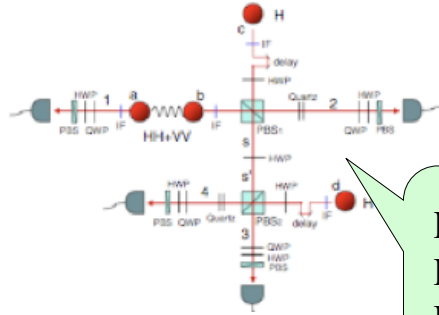
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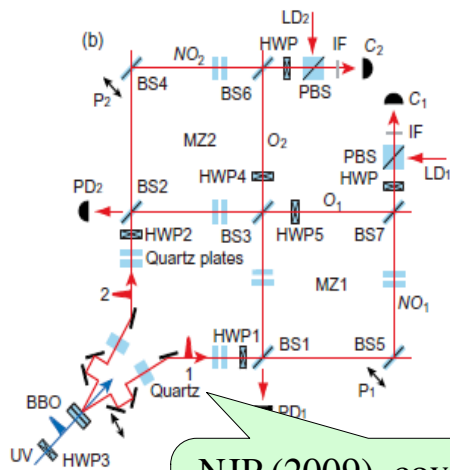
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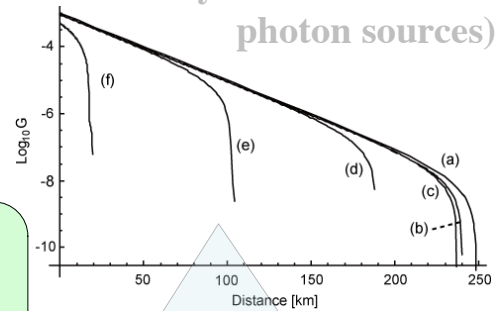
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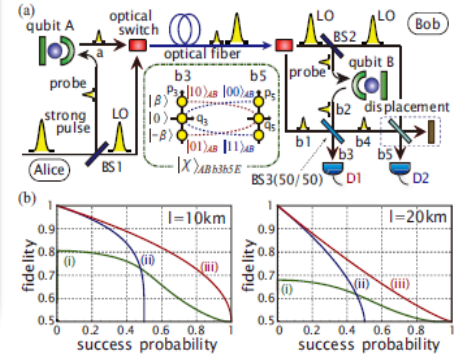
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Optimal design for quantum repeaters



Weak measurement . . .

You can tune the strength of a measurement by changing either the magnitude of interaction gt or the state of the meter. (for example, αgt for J-C, and $\alpha \chi^{(3)} L$ for Kerr QND)

When the measurement becomes weaker, the backaction becomes smaller, and the measurement error goes larger.

Thus *a single* weak measurement has no meaning, but if repeated measurements are allowed, the average of an observable can be obtained as precisely as you want (still, without causing back-action).

Therefore, the average of an observable inside an interferometer can be measured without affecting the interference.

Weak value ···

When you fix (select) the initial state and the final state, the output of a weak measurement *on the way between the initial and final states* is called **weak value**.

An interesting thing occurs when the selected initial and final states are non-orthogonal. The value can be outside of the spectrum of the physical quantity.

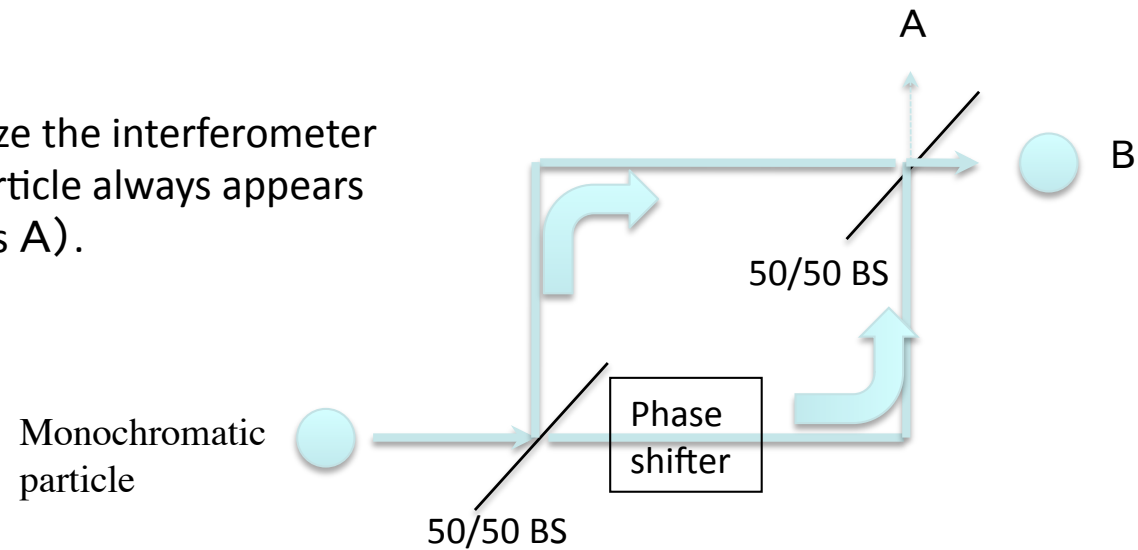
Especially, in Hardy's paradox, Aharonov predicted that **$\text{prob}(A)=1$ and $\text{prob}(B) =1$ and still $\text{prob}(A \cap B)=0$!!!**

We experimentally demonstrated that Aharonov's prediction is correct. The experiment became possible by

- photon-version of Hardy's paradox, and**
- joint weak measurement by means of entangled meters.**

Mach-Zehnder interferometer

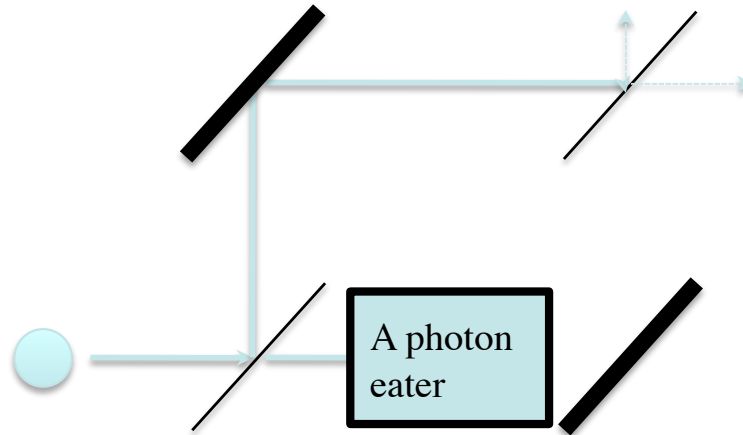
You can stabilize the interferometer
So that the particle always appears
In B (or always A).



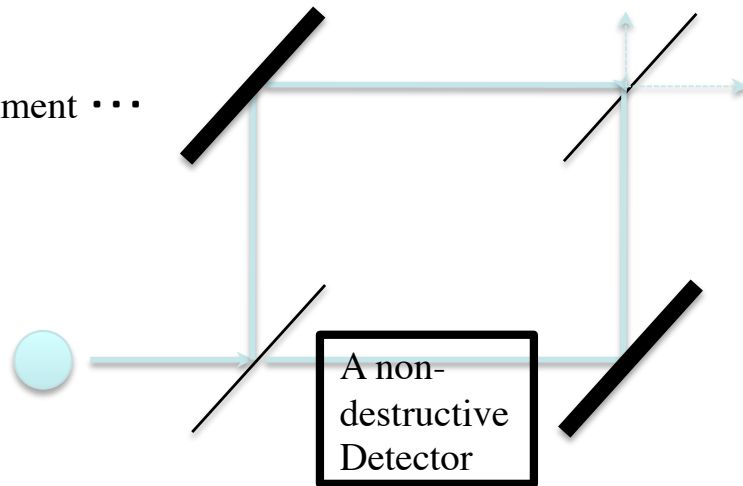
In this situation, you cannot say anything about "which path?".

Any attempt to look inside destroys interference

regardless whether it is a
destructive measurement ...

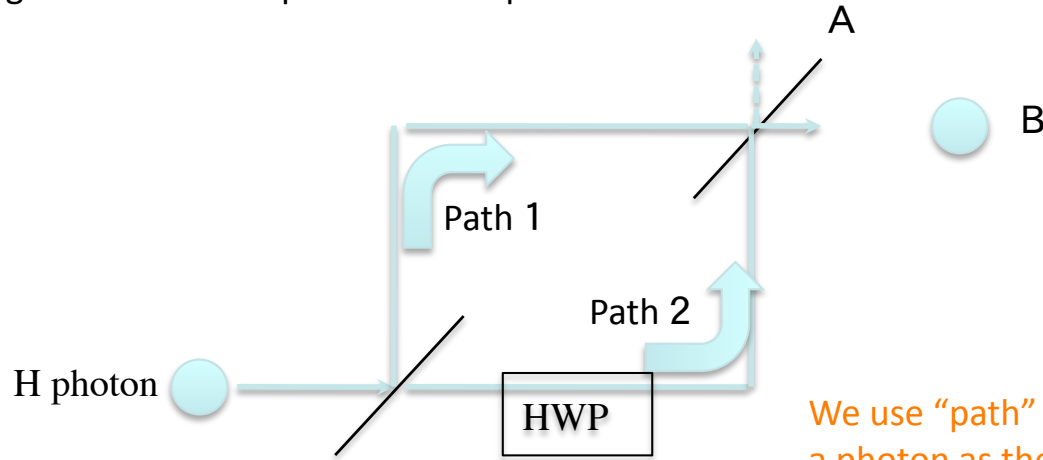


or, a non-destructive measurement ...



Polarization rotator can change “path qubit” into “polarization qubit.”

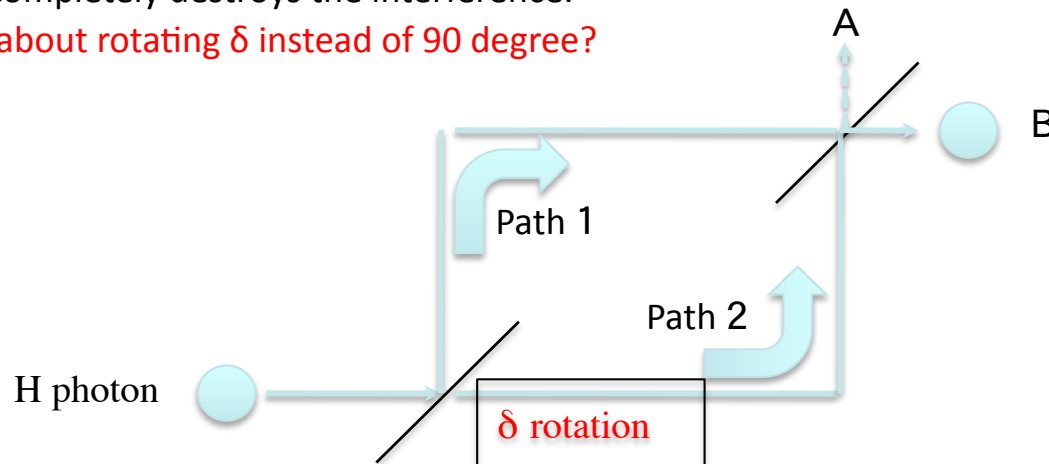
A HWP can change the incident H photon into V photon.



We use “path” and “polarization” of a photon as the “meter” and “system” qubits.

This completely destroys the interference.

How about rotating δ instead of 90 degree?

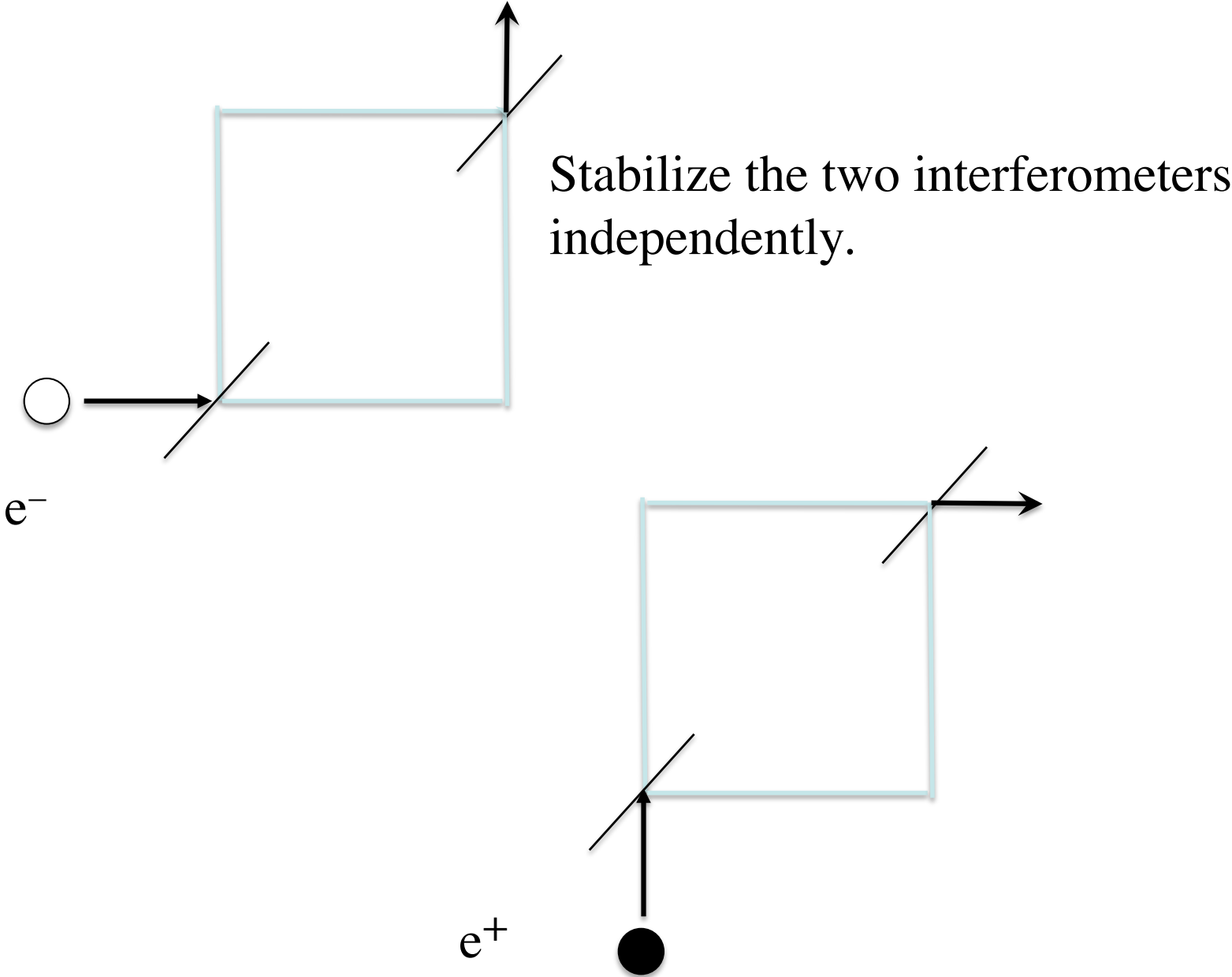


This almost does not destroys the interference, but the path distinguishability is also poor.

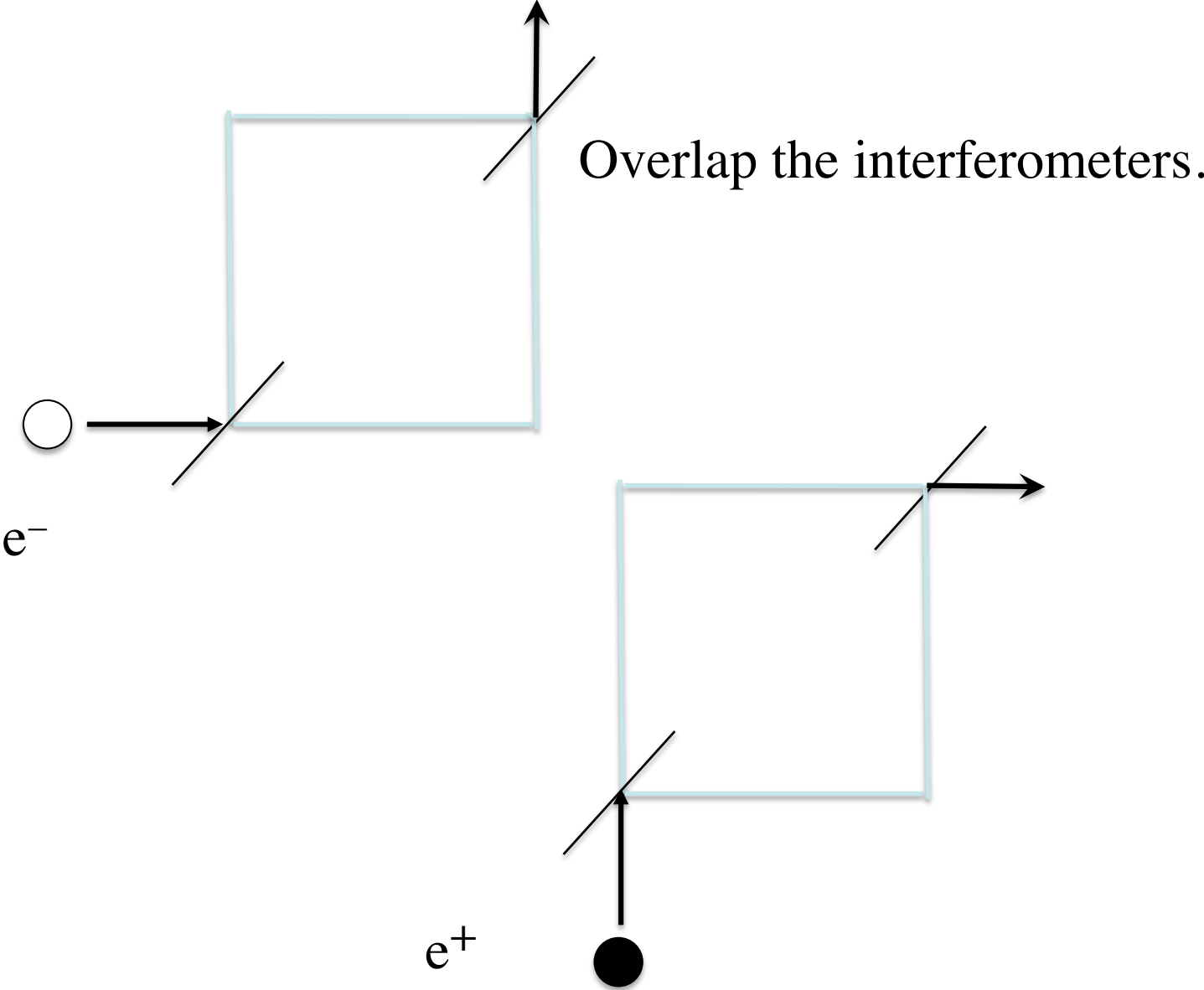
Repeating the measurement \rightarrow weak measurement

In this simple MZ interferometer, the answer is normal: $p = 1/2$ each.

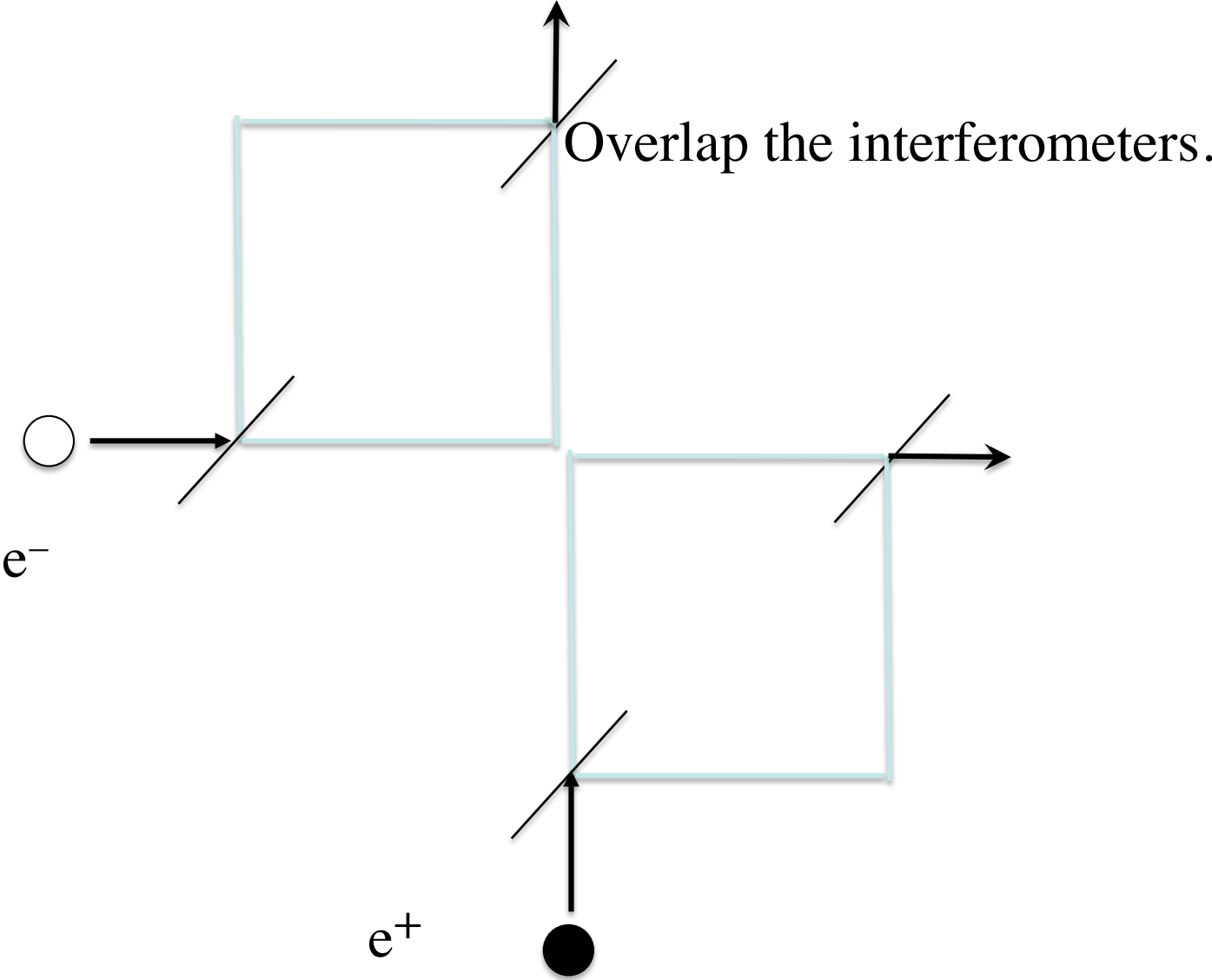
Hardy paradox



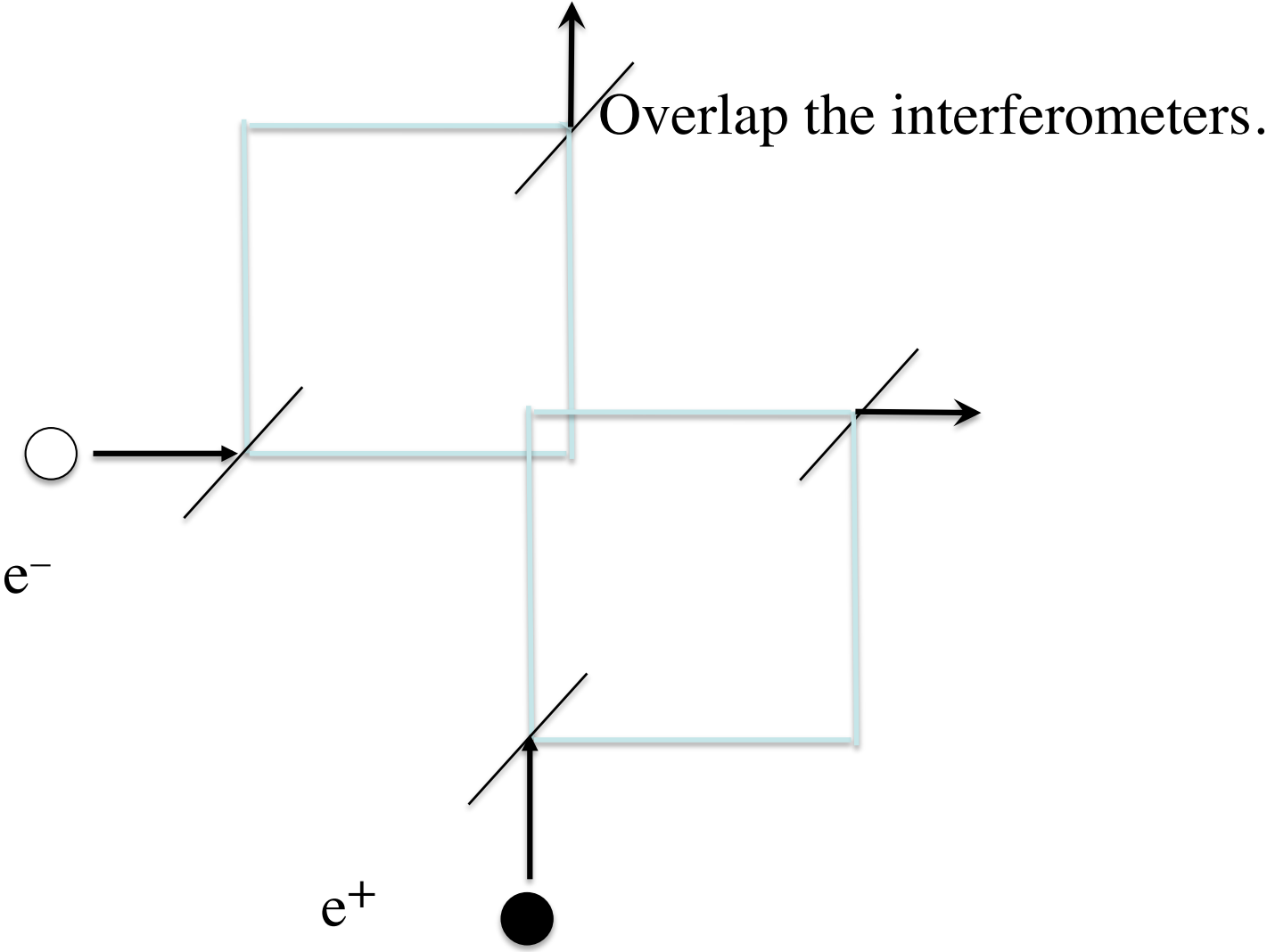
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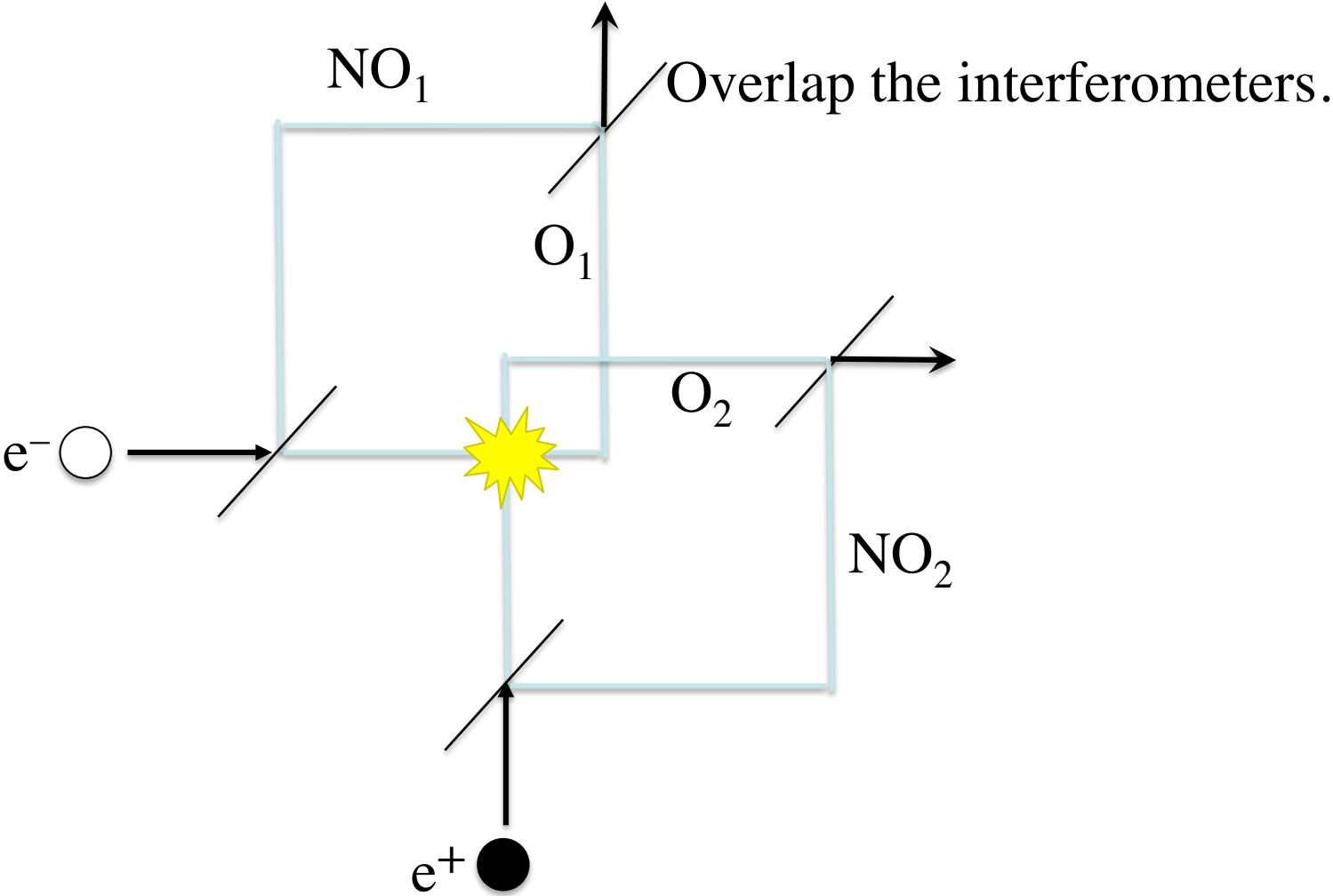
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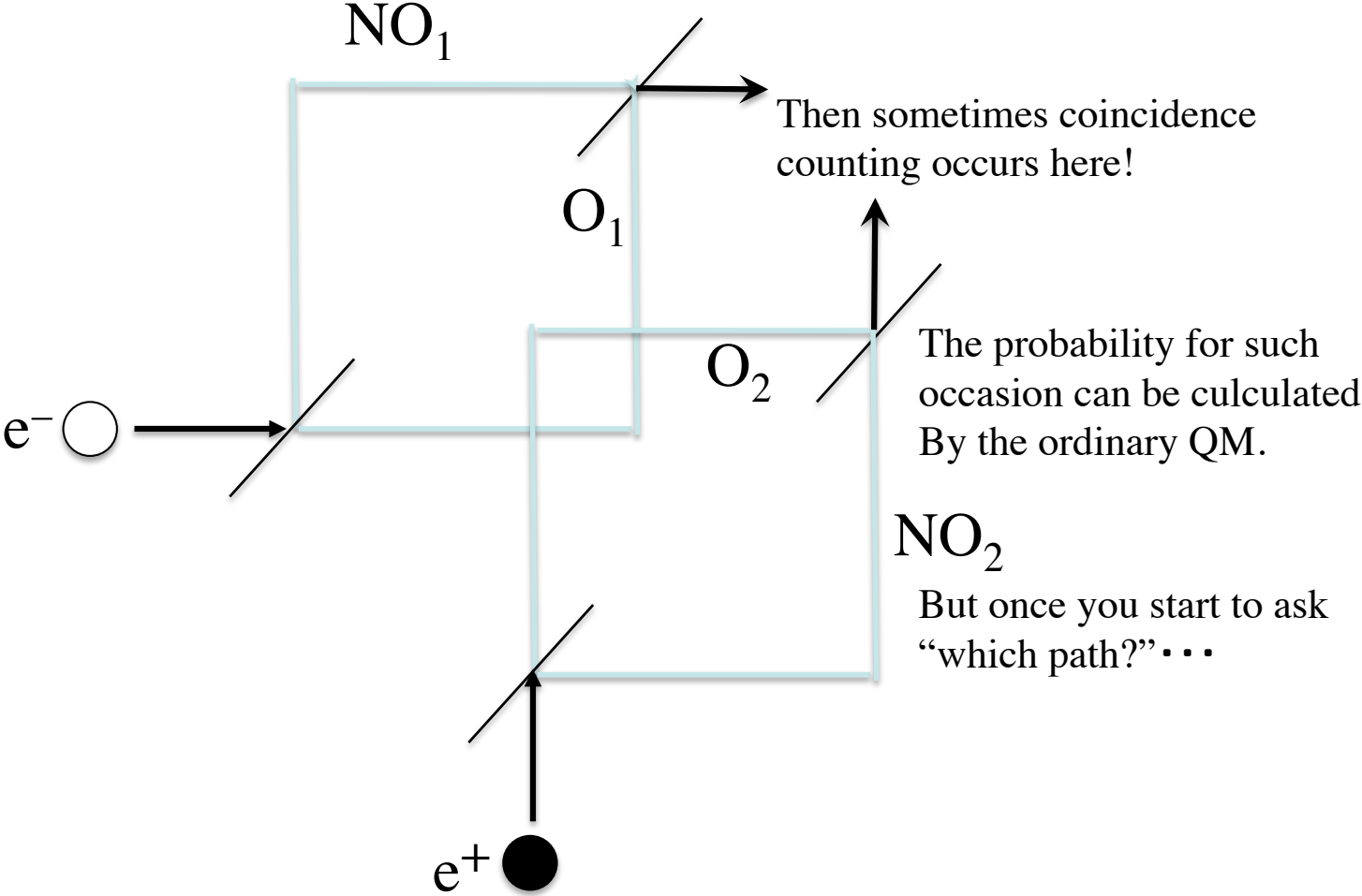
Hardy paradox



Hardy paradox

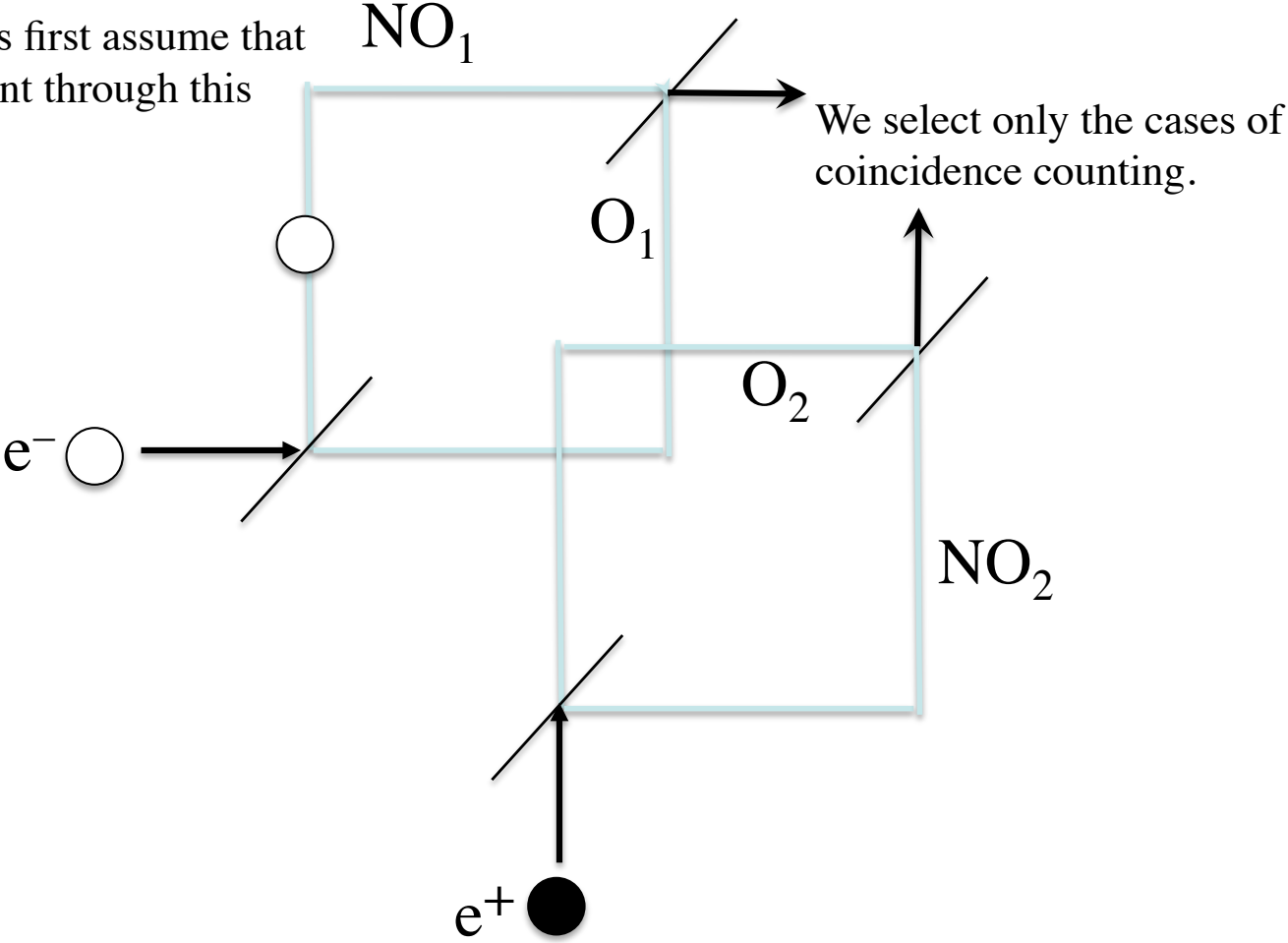


Hardy paradox



Hardy paradox

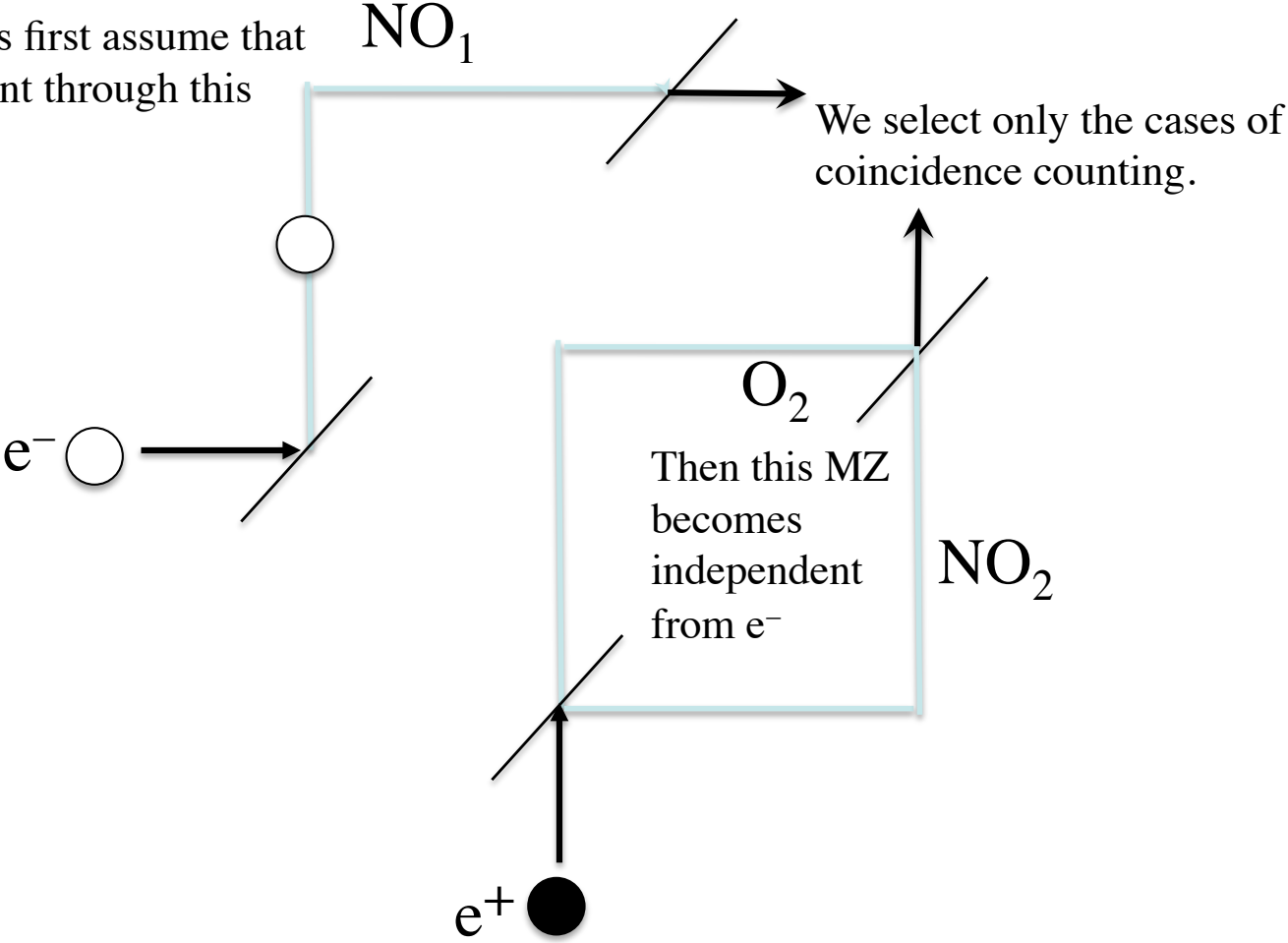
Let us first assume that e^- went through this path.



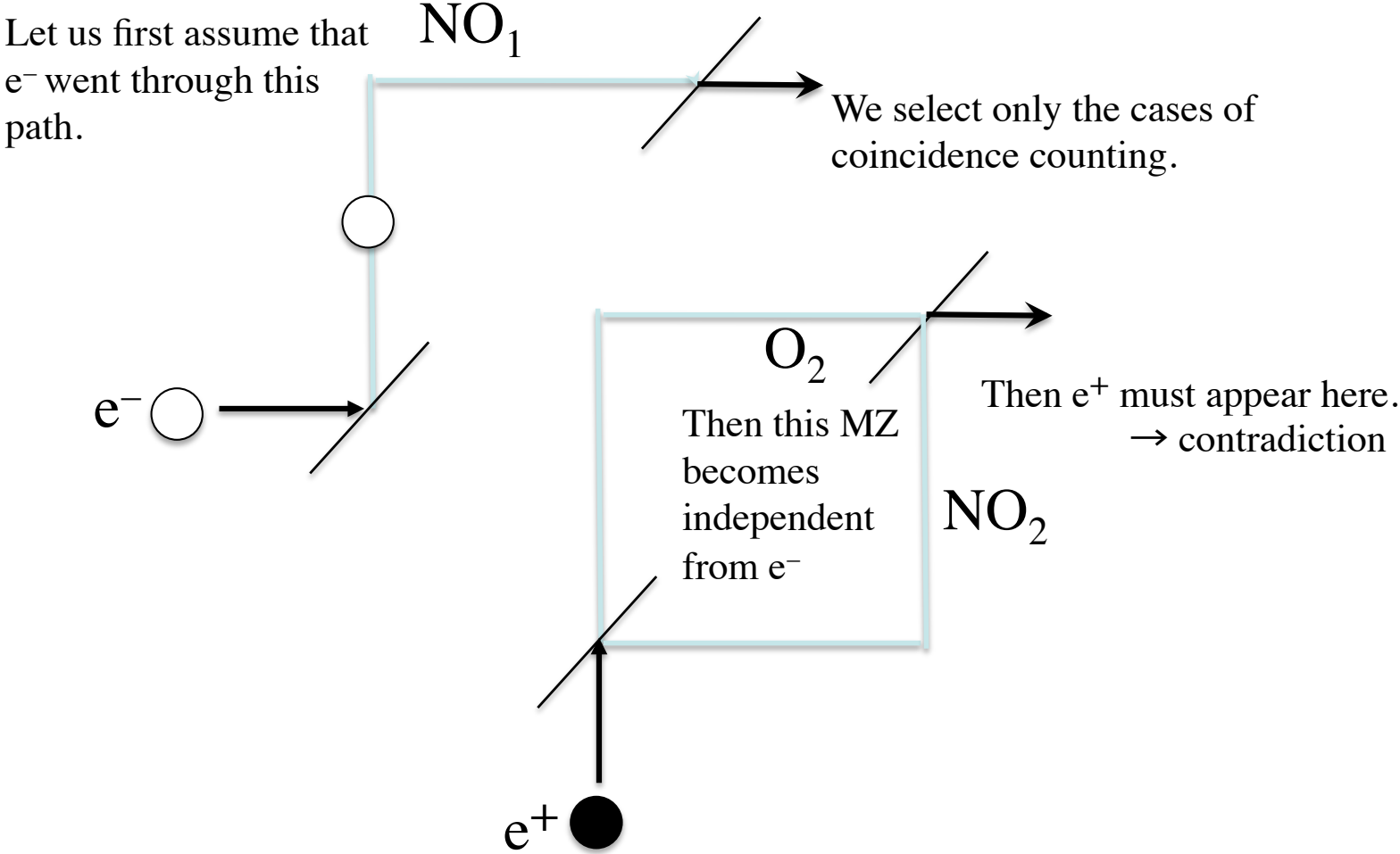
We select only the cases of coincidence counting.

Hardy paradox

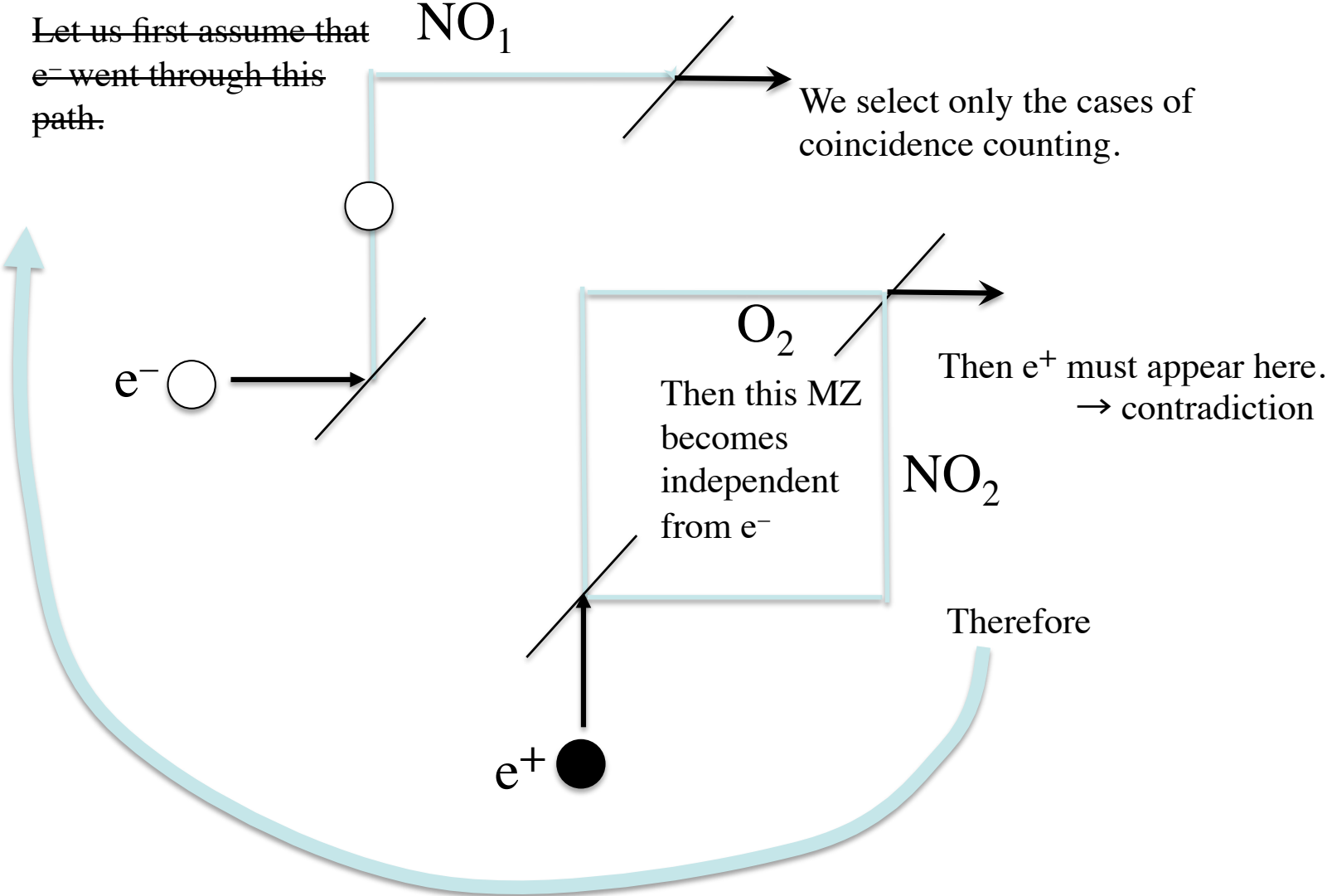
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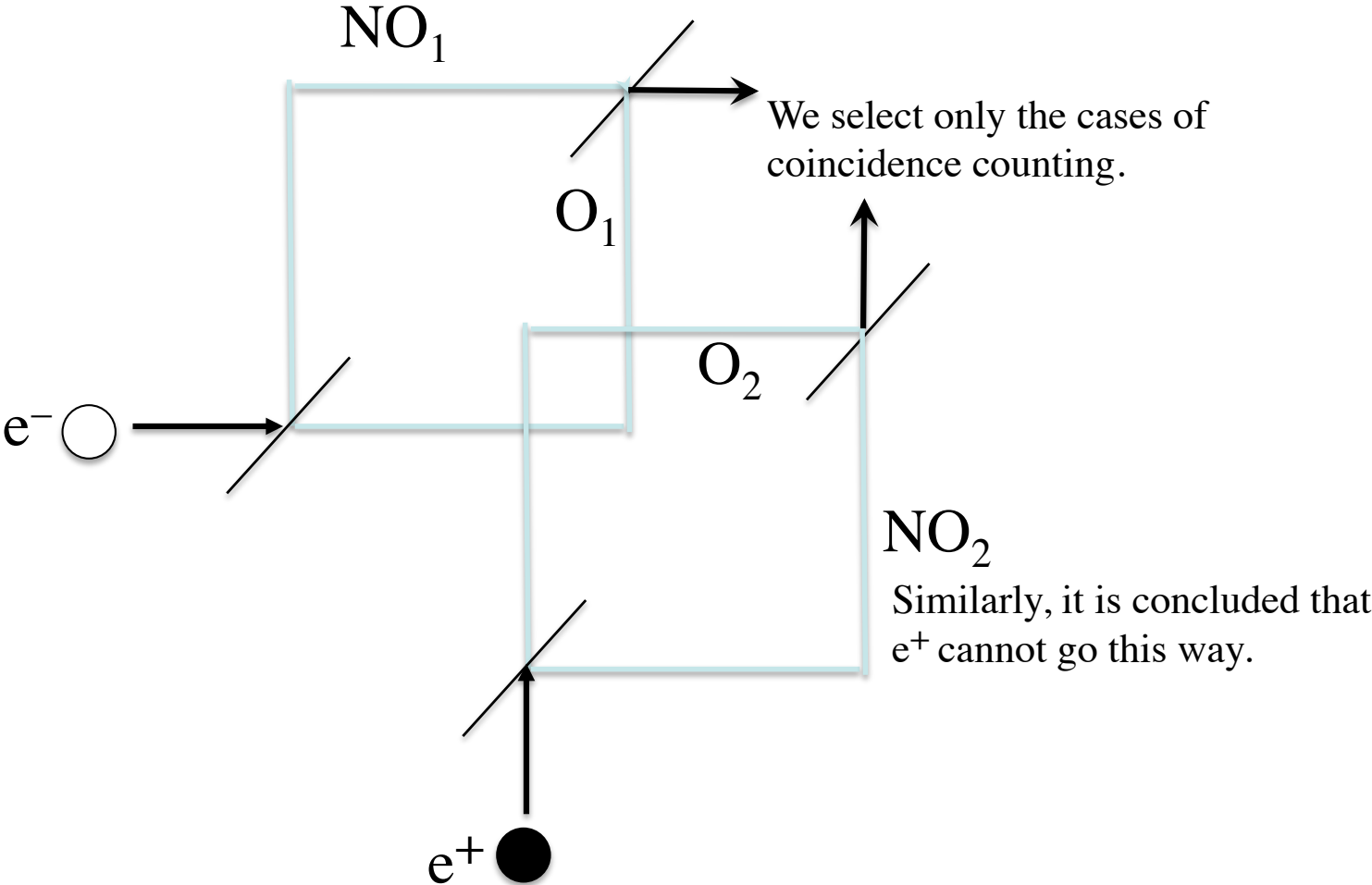
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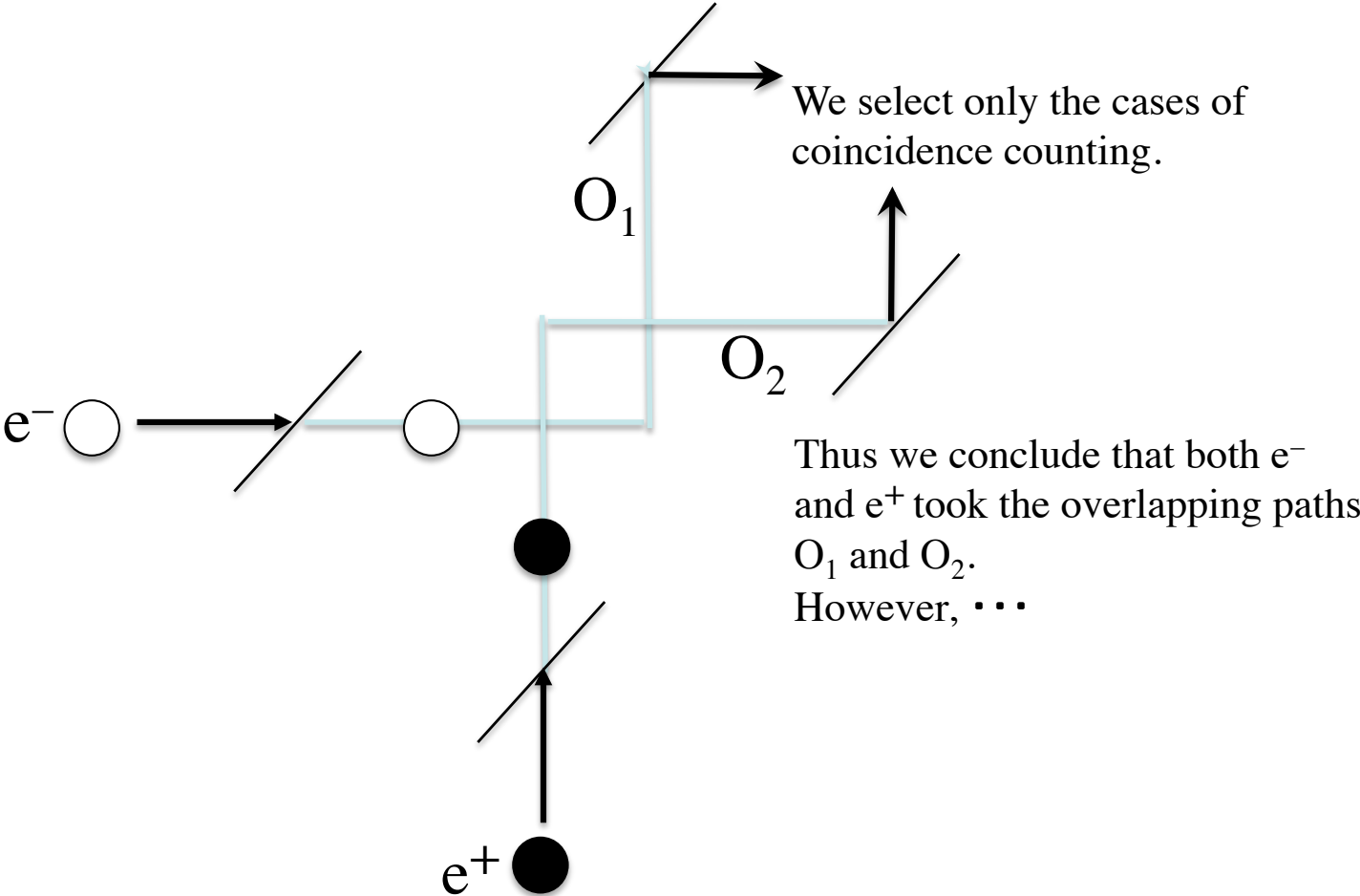
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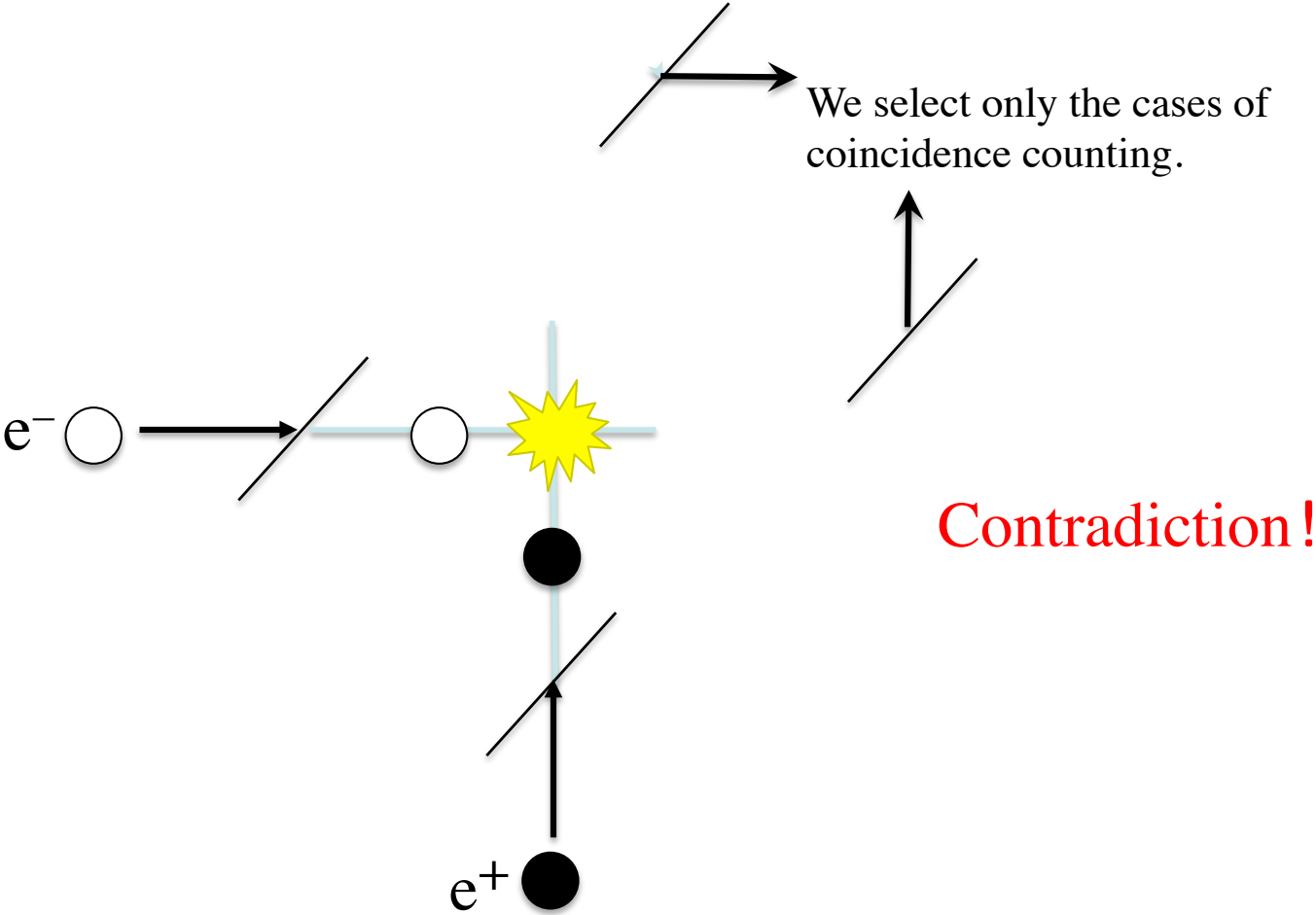
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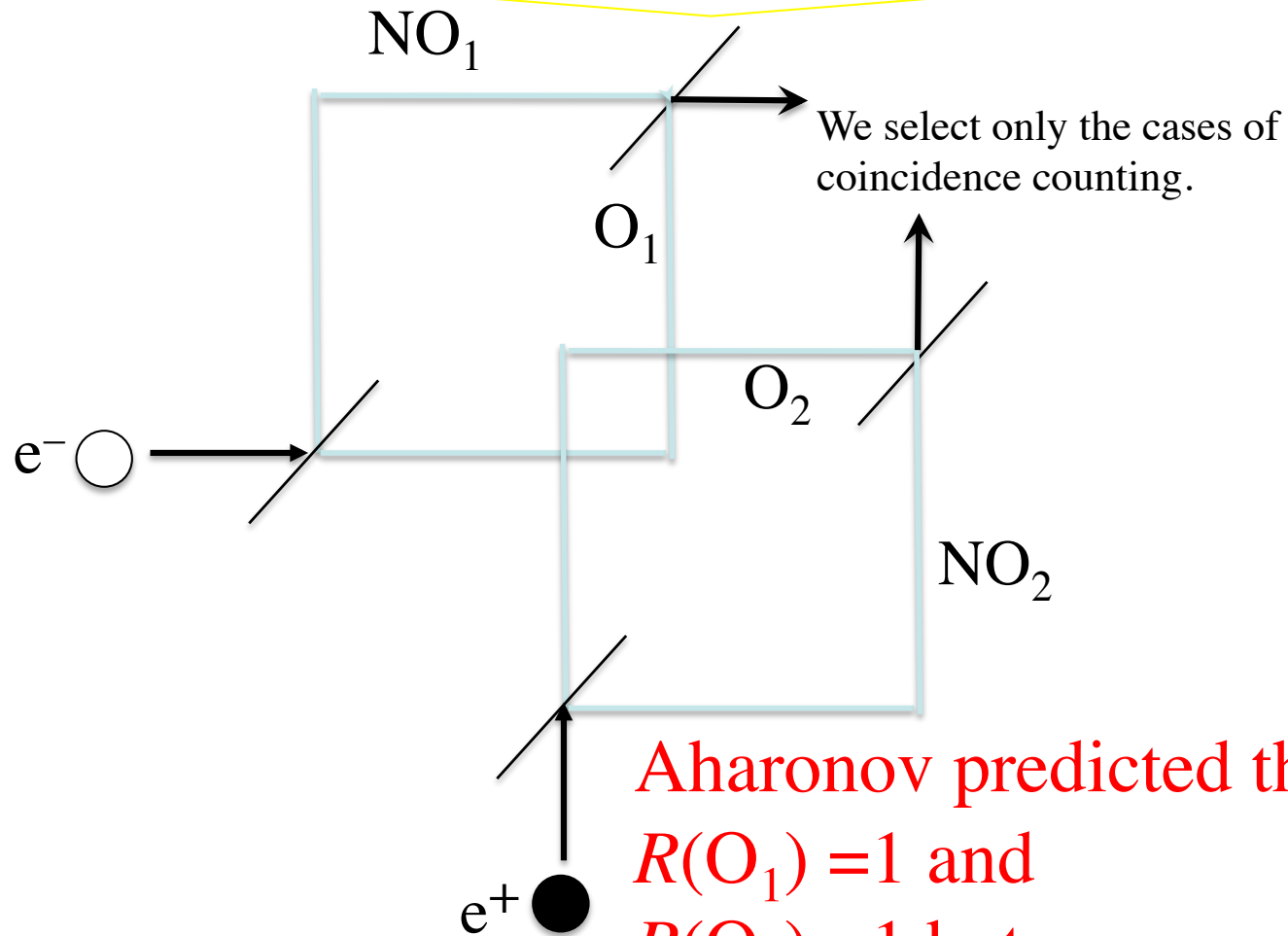


Hardy paradox

I told you. You should not ask “which path?”

Be satisfied with getting the transition probability.

No, we can make “weak measurement”!



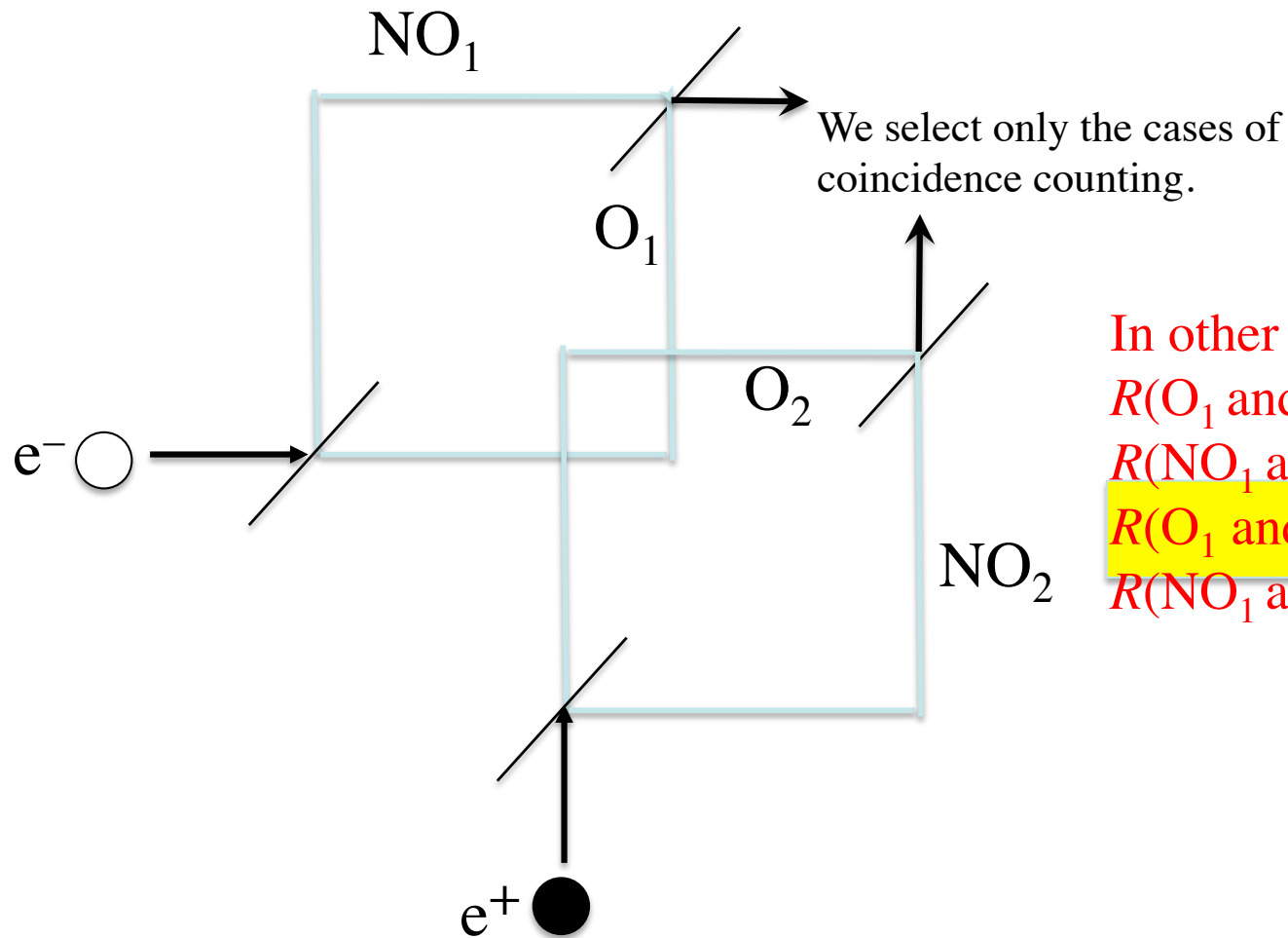
Aharonov predicted that

$$R(O_1) = 1 \text{ and}$$

$$R(O_2) = 1 \text{ but}$$

$$R(O_1 \text{ and } O_2) = 0$$

Hardy paradox



In other words,
 $R(O_1 \text{ and } NO_2) = 1$ and
 $R(NO_1 \text{ and } O_2) = 1$ and
 $R(O_1 \text{ and } O_2) = 0$ and
 $R(NO_1 \text{ and } NO_2) = -1$

$$R(O_1) = R(O_1 \text{ and } O_2) + R(O_1 \text{ and } NO_2) = 1$$

$$R(O_2) = R(O_1 \text{ and } O_2) + R(NO_1 \text{ and } O_2) = 1$$

$$R(NO_1) = R(NO_1 \text{ and } O_2) + R(NO_1 \text{ and } NO_2) = 0$$

$$R(NO_2) = R(O_1 \text{ and } NO_2) + R(NO_1 \text{ and } NO_2) = 0$$

Sunday May 31st 2009

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Science & Technology

Physics and philosophy

I'm not looking, honest!

Mar 5th 2009

From *The Economist* print edition

The good news is reality exists. The bad is it's even stranger than people thought

"HOW wonderful that we have met with a paradox. Now making progress." So said Niels Bohr, one of the founders. Since its birth in the 1920s, physicists and philosophers have explored the bizarre consequences that his theory has for reality, including the truth that it is impossible to know everything about the world, whether it really exists at all when it is not being observed. Physicists, working independently, have demonstrated that particles exist when unobserved. When no one is peering, however, it

In the 1990s a physicist called Lucien Hardy proposed a theory that makes nonsense of the famous interaction between matter and antimatter when a particle meets its antiparticle, the pair always annihilates in a burst of energy. Dr Hardy's scheme left open the possibility that when their interaction is not observed a particle and an antiparticle can exist with one another and survive. Of course, since the interaction is unobserved, no one should ever notice this happening, which is known as Hardy's paradox.



MAY 5, 2009

Science, Spirituality, and Some Mismatched Socks

Researchers Turn Up Evidence of 'Spooky' Quantum Behavior and Put It to Work in Encryption and Philosophy

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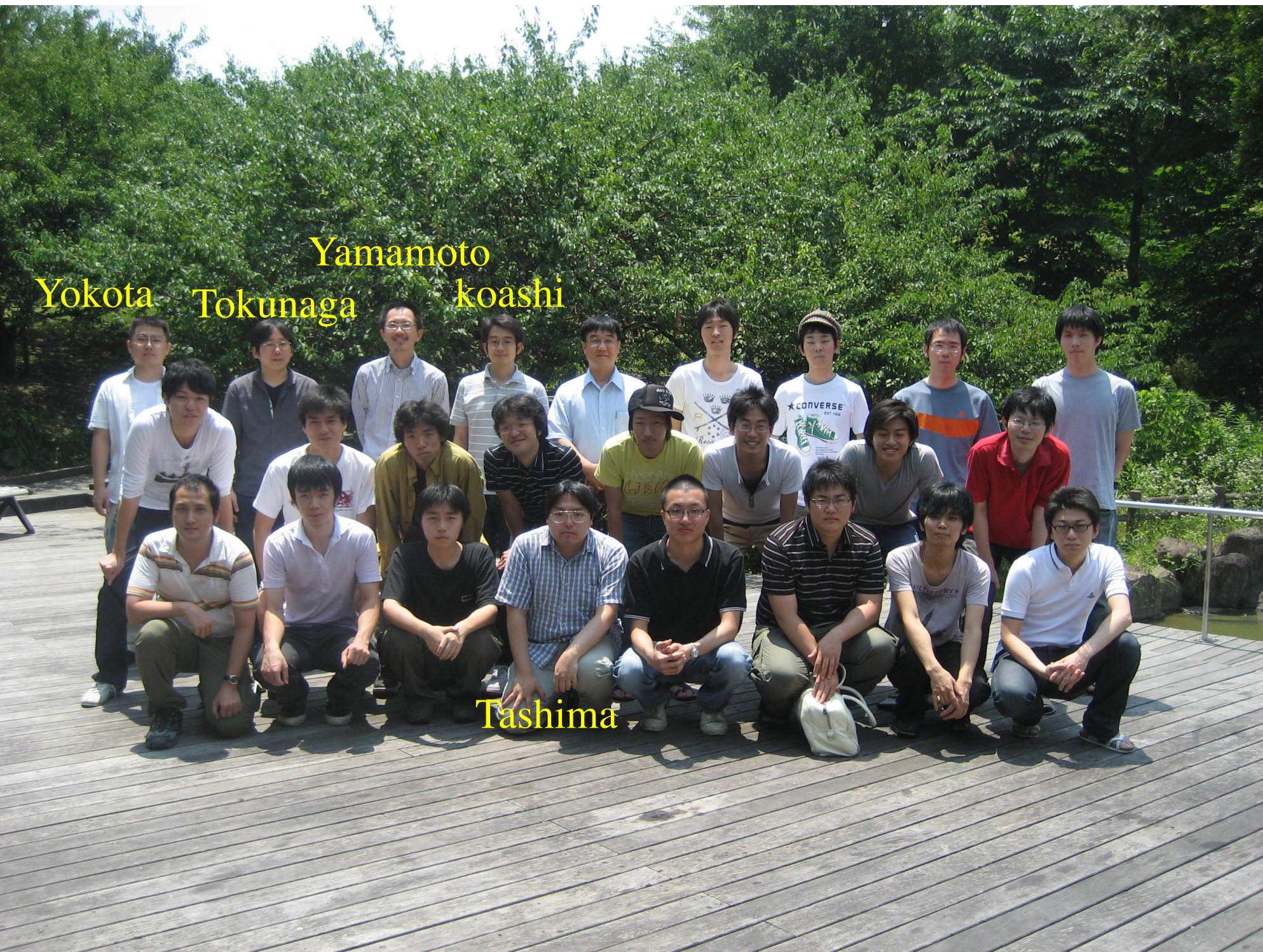
- Text +

By GAUTAM NAIK

One of quantum physics' crazier notions is that two particles seem to communicate with each other instantly, even when they're billions of miles apart. Albert Einstein, arguing that nothing travels faster than light, dismissed this as impossible "spooky action at a distance."

In a striking achievement, scientists from Osaka University have resolved the paradox. They used extremely weak measurements -- the equivalent of a sidelong glance, as it were -- that didn't disturb the photons' state. By doing the experiment multiple times and pooling those weak measurements, they got enough good data to show that the particles didn't annihilate. The conclusion: When the particles weren't observed, they behaved differently.

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Yamamoto

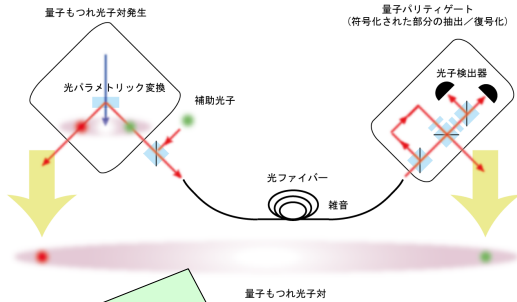
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Tashima

Our recent activities

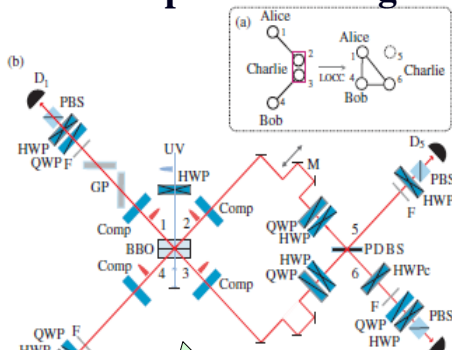
Theory and experiments

Protection of entanglement using DFS (decoherence-free subspace)



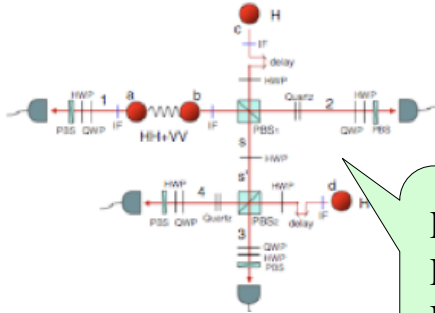
Nature (2003), PRL (2005)
NJP (2007), Nature Photonics (2008)

Fusion gates and expansion gates For multipartite entanglement



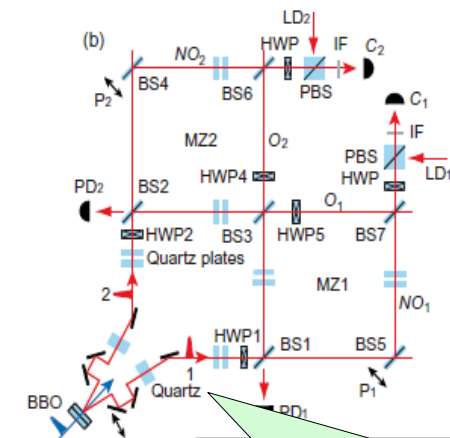
PRL (2009), PRA (2009)
NJP (2009), PRA (2008)

Cluster-state one-way Quantum computing



PRL (2008)
PRA (2006)
PRA (2005)

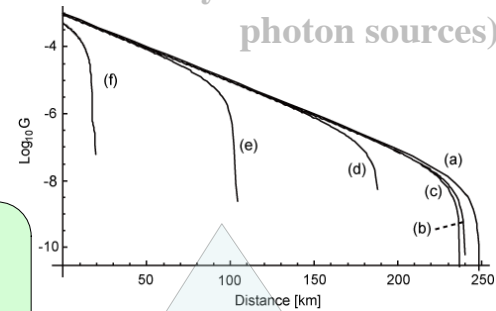
Experimental verification for Aharonov's anomalous weak value



NJP (2009), covered by
The Economist
Wall Street Journal

Theory

QKD security proof: general theory and for non-ideal photon sources



PRL(2007), PRA(2009)

PRA (2010)
PRA (2009)

Optimal design for quantum repeaters

