

# Anomalous propagation of EM waves in structured metamaterial

Hiroharu Tamaru

Photon Science Center  
The University of Tokyo



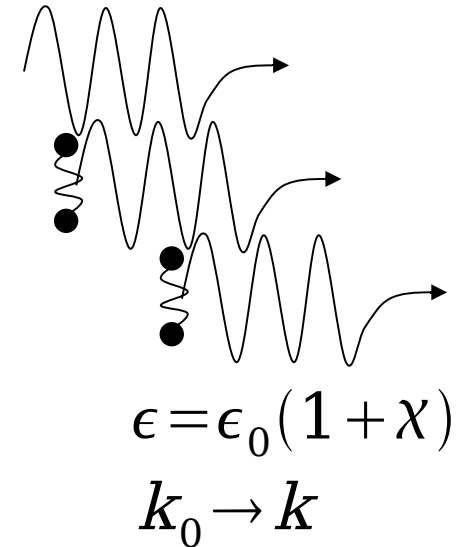
<http://psc.t.u-tokyo.ac.jp/>



- Highly conceptual discussion  
struggling to see the “anomalous propagation”  
in a “normal” way.
  - more of a 'call-for-discussion' than a talk
- To begin from the very end:  
I would like to shed more light on  
“confined states” (resonators)  
when we talk about propagation
  - views of phenomena as  
phase interferences of propagators & resonators

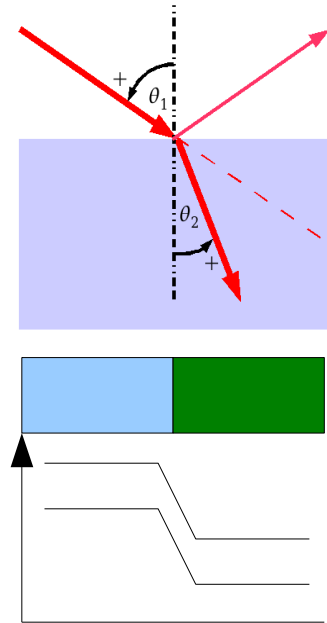
# Propagators (extended modes)

- plane waves (propagators)
  - periodic or uniform system
  - **electronic**: crystals: band diagram
  - **photonic**: permittivity and permeability
- They were and are important:
  - extraction (detection) are with propagators:
    - electric currents (dc/ac), light beams
  - numerous “confined states” are renormalized into small number of propagators -> analytical soltn.
    - the rest (nearfields) of the “confined states” can be forgotten



# Boundaries

- photonic interface:
  - Snell's law, Fresnel formula, ....  
relation between propagators at the interface
- electronic interface: as in diodes  
.... more conceptual cf. decoherence



## At the bleeding edge:

nano-optics, structured media, ultrafast dynamics ...

--- full of boundaries, in space and time

analysis involves large number of propagators:

very-high-order components of Fourier spectra ( $k, \omega$ )  
and with dispersion taken into account

Why expansion, when they are accumulated again?

---> resonators

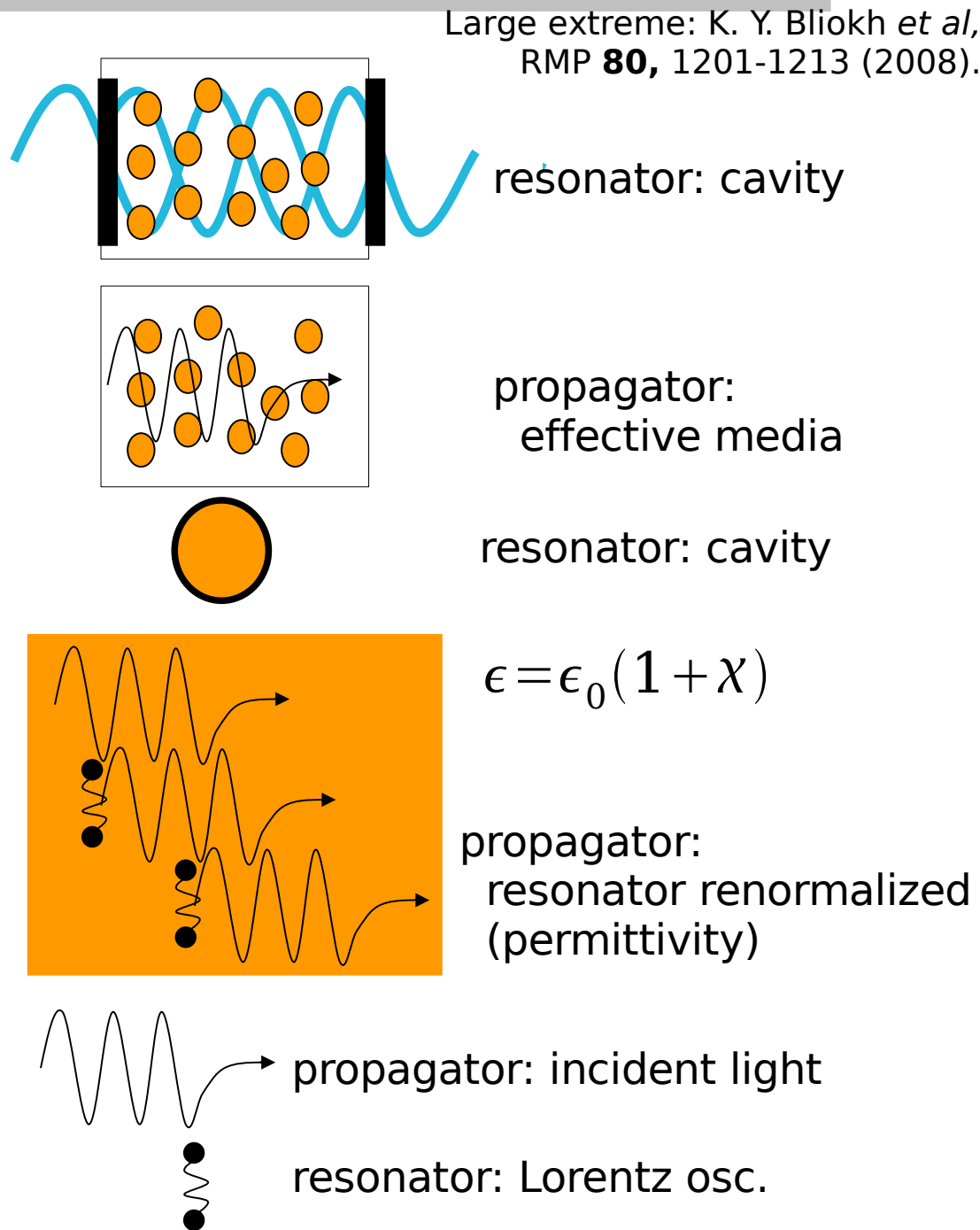
# Layering of resonators and propagators

- mutual layering of resonators and propagators
- Propagator: delocalized, indexed by  $\mathbf{k}$
- Resonator: localized, indexed by  $\omega_0$
- carriers of phase, where it is open - propagator or feedback - resonator

relevance for coupled state

0  
Q  
 $\infty$

$\omega_0$



# S.Foteinopoulou (2003)

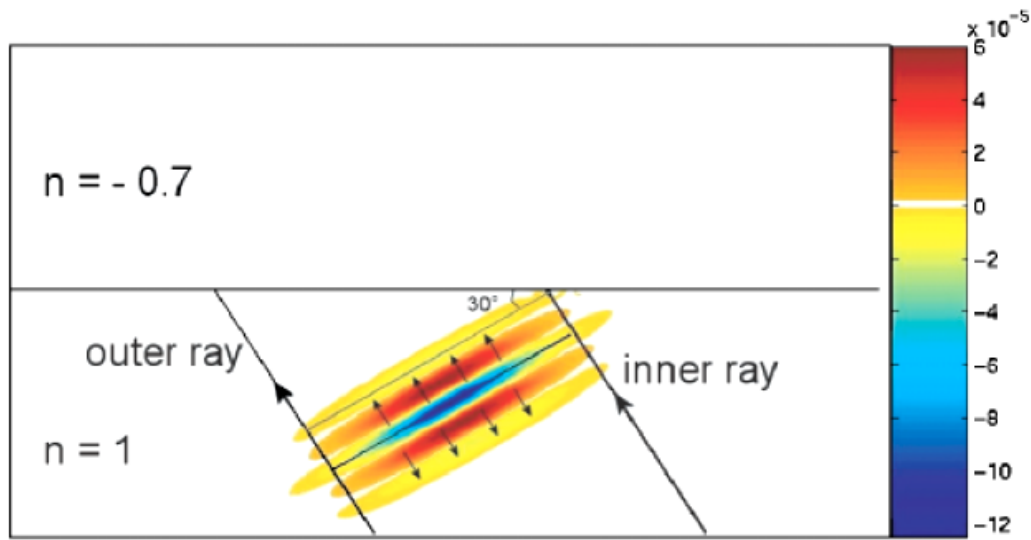
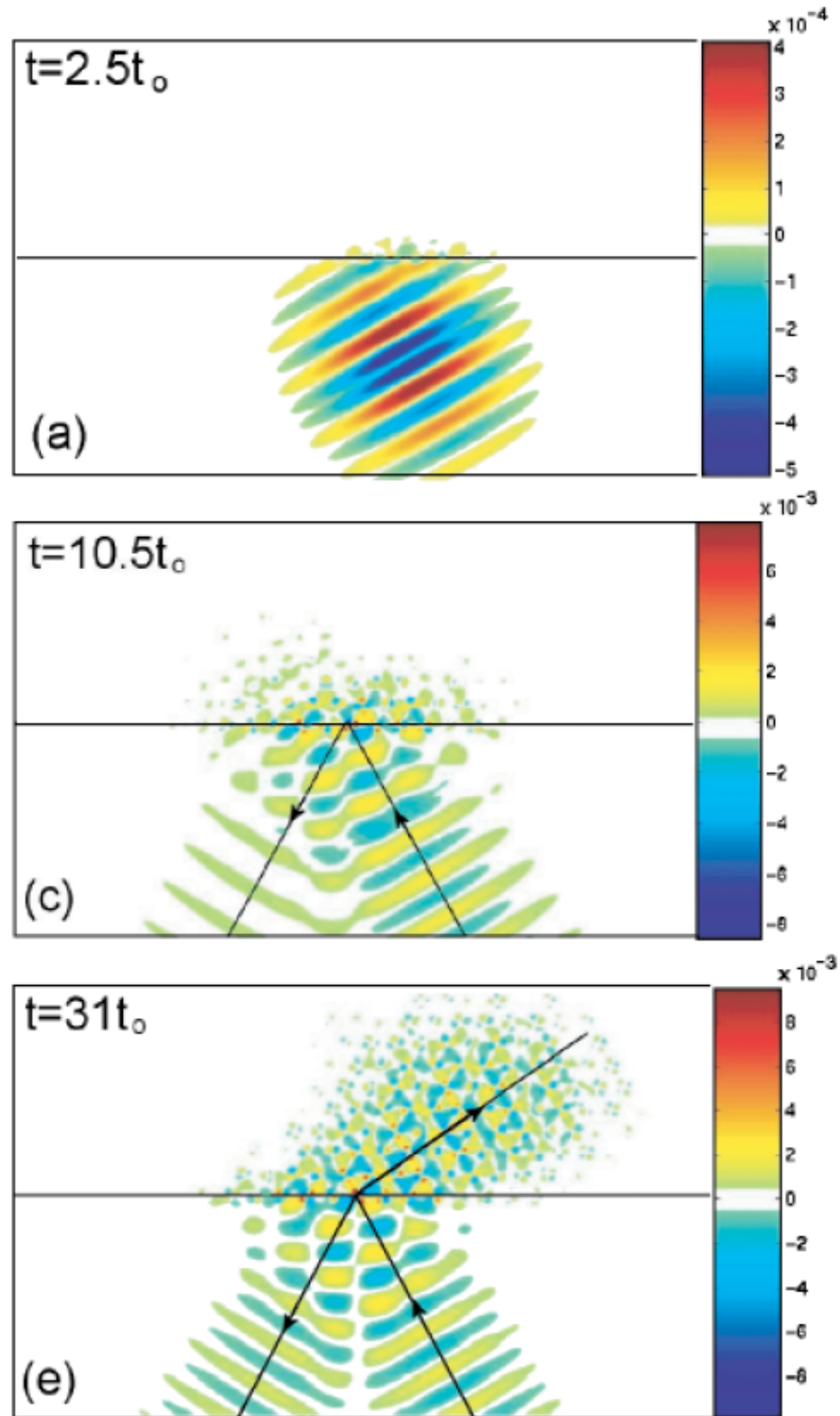


FIG. 2 (color online). An incident EM wave is propagating along a  $30^\circ$  direction. The time is 200 simulation steps.



# F.J.Rachford (2002)

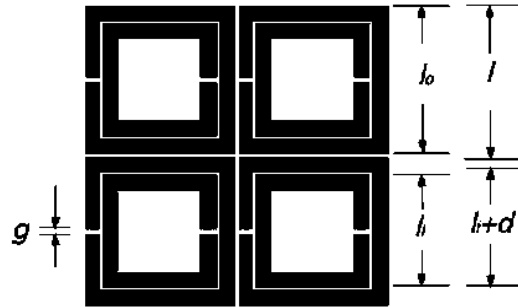
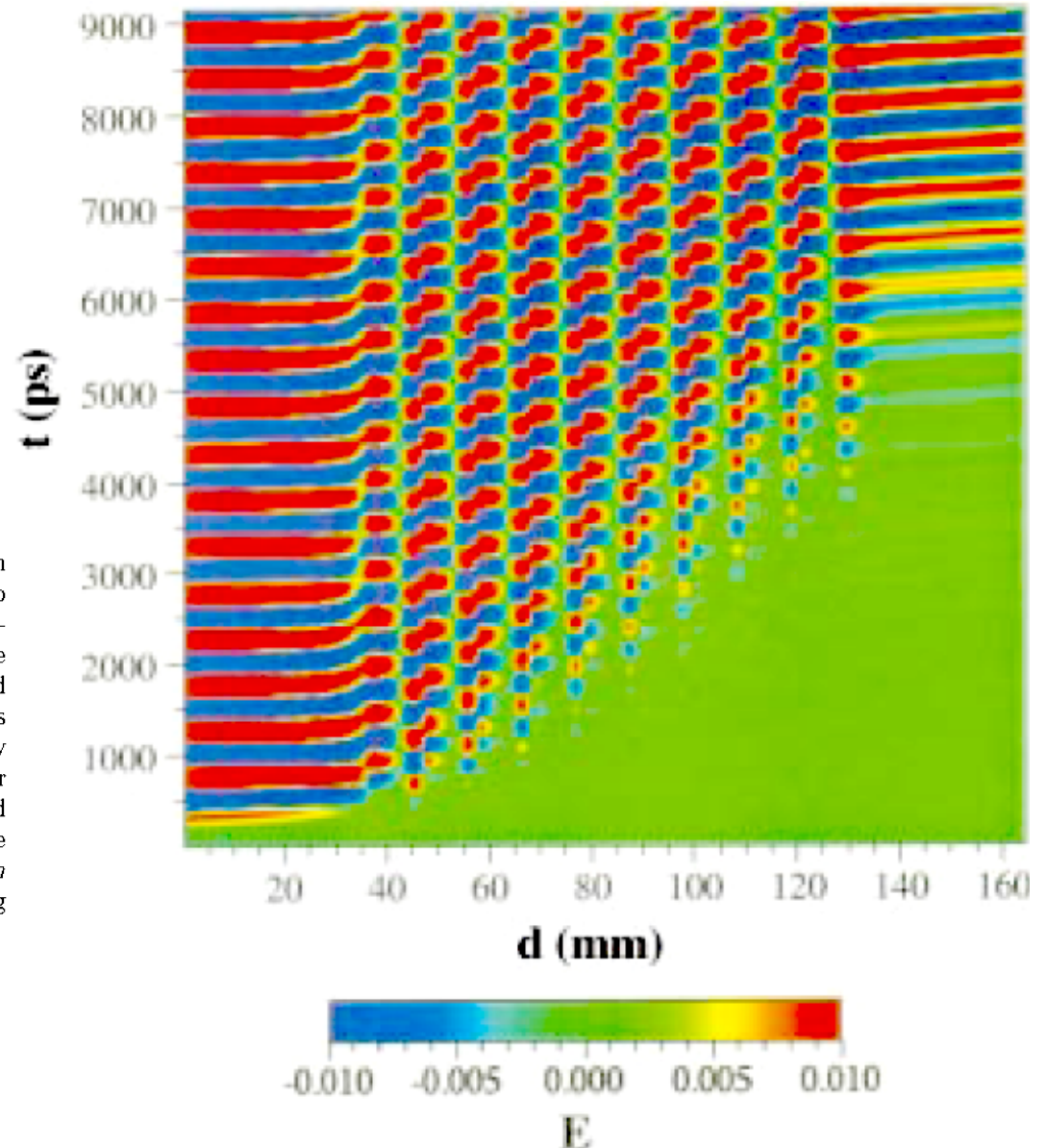


FIG. 1. Square double ring geometry. Lattice constant  $l = 1.04$  cm, ring's outer dimensions  $l_o = 0.99$  cm, etched linewidth 1 mm, inner ring's outer dimensions  $l_i = 0.75$  cm, inter-ring gap of 0.2 mm, and ring gap  $g = 0.04$  cm.

FIG. 4. (Color) Propagation of 1.96-GHz microwave radiation through our ring/wire composite media. A plane wave is assumed to enter from the left. Time is plotted on the vertical axis while distance is plotted on the horizontal axis. From 0 to 35 mm the wave is in free space. The wave enters the ring/wire medium with  $E$ -field polarization along the direction of the wires. It takes several cycles before the resonant response of the medium settles into a steady state. At 129 mm, the radiation exits from the medium. The color scale is saturated to highlight the position of successive  $E$ -field crests and troughs. In this case resonances at the ring locations are pronounced and the apparent index of refraction is ambiguous:  $n = +11.8$  is for rising phase slope and  $n = -3.6$  for decreasing phase slope.



# Phase interference

---

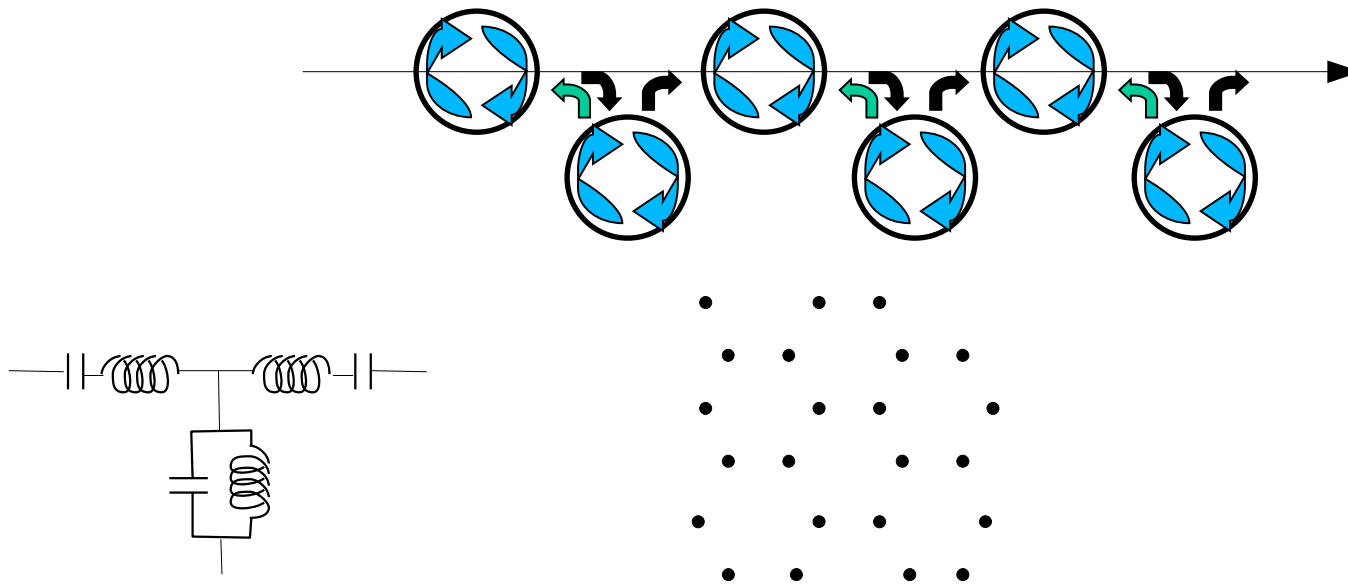
- “Functions” of a system:  
    results of interferences of phase
- Propagators do not interfere with each other:  
    propagator interferes with resonators, and  
    resonators interferes with multiple propagators  
    – scattering, reflection, refraction...  
    -> these are easier to renormalize into  
    propagator - propagator interaction
- The more interesting are:  
    “double-resonator” systems



# Double resonators

Under this framework, most of the interesting phenomena are in “double resonator” systems:

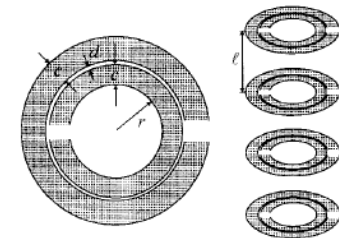
- Band crossing (in contrast to anti-crossing):
  - CRLH-Transmission line
  - electronic band structure of graphene
- > Two “tuned” resonators with different topology



# Double resonators

- Negative refractive index
  - Split ring resonator
    - electronic (metal material)
    - photonic (ring structure)
  - Photonic crystal with backward wave
    - photonic (particle itself)
    - photonic (periodicity, Bloch, Umklapp)
- > Two strong just-above-resonance resonators with different topology

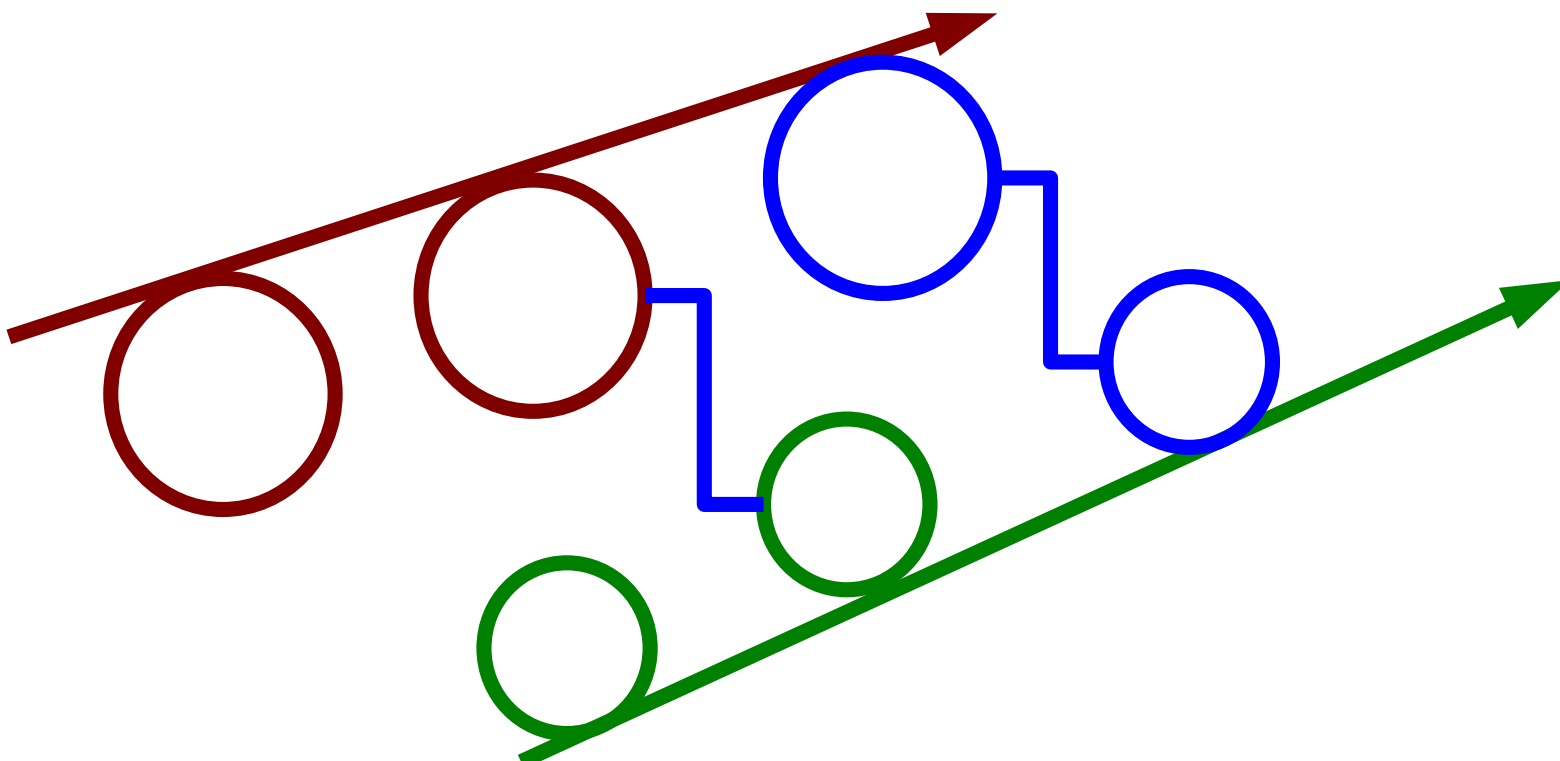
J. B. Pendry, et al., *IEEE T Microw. Theory* **47**, 2075 (1999).



cf: crystal themselves are “double resonance”

# “Anomalous” propagation

- “Anomalous” effects tend to occur when resonators that are renormalized into propagators independently, start to interact “directly”.
  - renormalization order has to be inverted



# Analogies?

---

- Resonators
  - Near-field
  - Voltage
  - Kinetic potentials
  - Scalar potentials
  - Position
  - Propagators
  - Far-field
  - Current
  - Kinetic energy
  - Vector potentials
  - Momentum
- ⋮
- ⋮

# Metamaterials

---

Metamaterials under this picture:

- Materials:  
systems with electronic resonators
- Photonic crystals:  
systems with photonic (incl. polaritonic, SPP)  
resonators
- Metamaterials:  
systems with electronic/photonic resonators

“Implementations” of the “abstraction” of phase-  
interaction network

# Terminology considerations

---

- electronic reso. + photonic prop. .... polaritons?
- photonic reso. + photonic prop. .... open cavity
- photonic reso. .... cavity, near-field photon
- electronic reso. + photonic reso. .... ?
  
- resonator + propagator .... ?

# Summary

---

- Conventionally, we are used to work with plane waves as our base, and have learned to renormalize all other effects into this “**propagator.**”

“**Resonators**” are the counterpart to propagators, which become more insightful when the system has more “space and time boundaries” than bulk.

- The pair is a candidate to make **abstraction** of materials and metamaterials under the same framework, in that “function” is abstracted by phase interaction, and the “carrier” of the phase (electrons, photons, polaritons, ...) is made implementation detail.